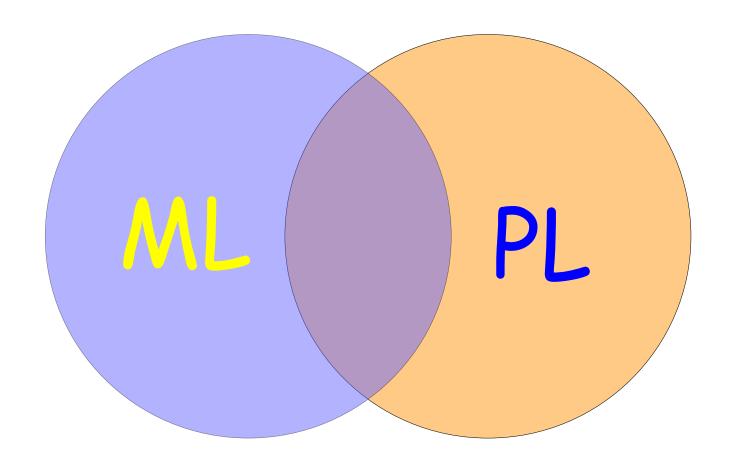
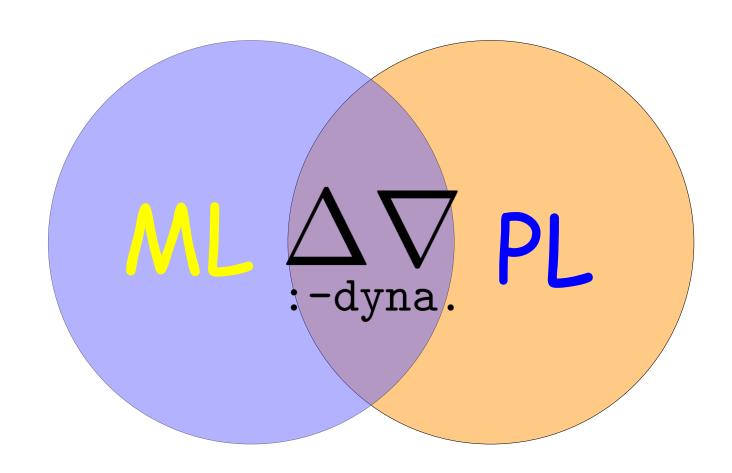
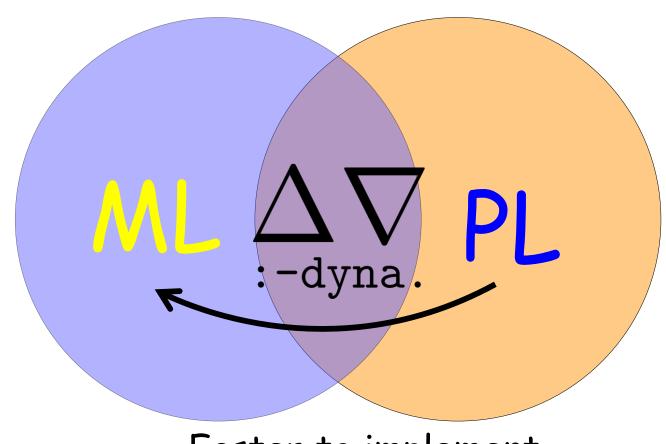


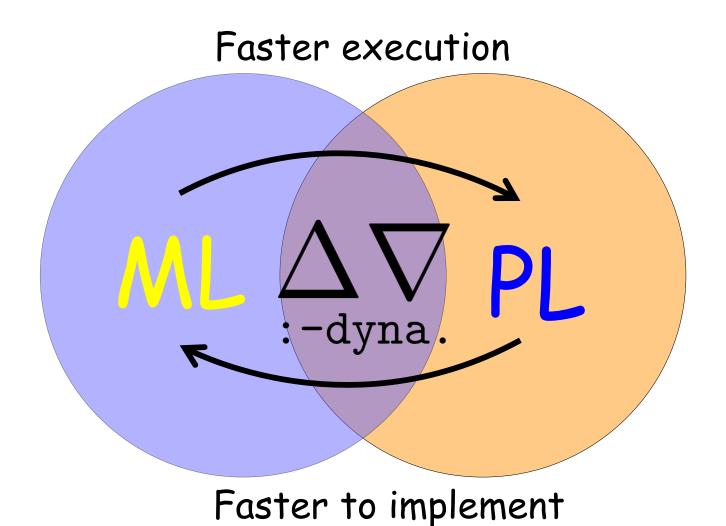
Tim Vieira, Matthew Francis-Landau, Nathaniel Wesley Filardo, Farzad Khorasani, and Jason Eisner

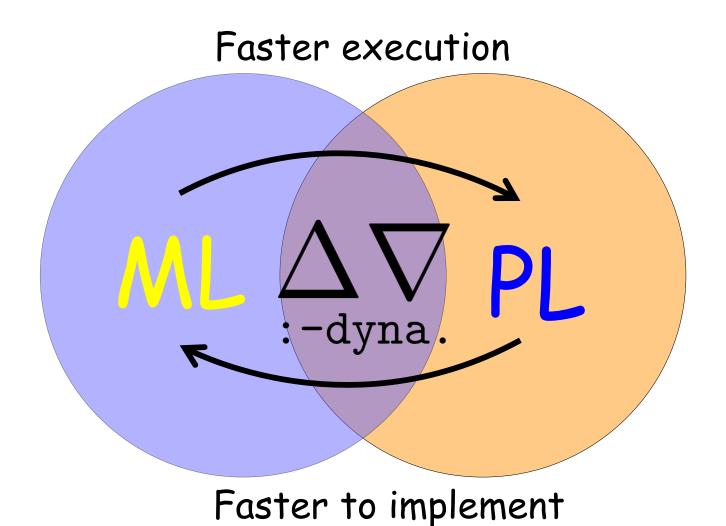






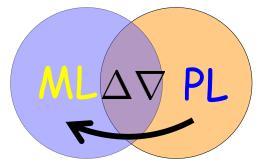
Faster to implement



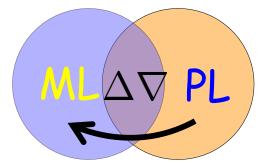


• Why Declarative Programming?

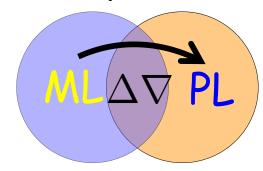
- Why Declarative Programming?
- Quick introduction to the Dyna language



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Automatic optimization of Dyna programs



A programming paradigm where the programmer specifies <u>what</u> to compute and leaves <u>how</u> to compute it to a solver.

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- Examples: SQL, Prolog/Datalog, Mathematica, Regex, TensorFlow/Theano
- Solver seeks an efficient strategy (e.g., SQL query planning)

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- Manually experimenting with all possibilities is time consuming
 - Programmers usually only implement one
- Researchers don't have time to optimize the efficiency of their code
 - We can do better with automatic optimization

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- Difficult to reliably discover long range interactions in a program

• Declarative language

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- Based on weighted logic programming

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What is Dyna?

- Declarative language
- Based on weighted logic programming
- Prolog / Datalog like syntax
 - Uses pattern matching to define computation graphs
- Reactive
- Dyna programs are close to their mathematical description
 - Similar to functional programs

a = b * c.

a will be kept up to date if **b** or **c** changes. (Reactive)

```
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a will be kept up to date if b or c changes. (Reactive)
b += x.
b += y. equivalent to b = x+y. (almost)
b is a sum of two variables. Also kept up to date.
```

c is a sum of <u>all</u> defined z(...) values.

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       a will be kept up to date if b or c changes. (Reactive)
b += x.
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      b is a sum of two variables. Also kept up to date.
c += z(1).
                                                 a "patterns"
                                                 the capitalized N
                                                 matches anything
c += z("four").
                             c is a sum of all
c \neq z (foo(bar, 5)).
                             defined z(...) values.
```

```
a(I) = b(I) * c(I).
```

pointwise multiplication

$$a(I) = b(I) * c(I).$$

$$a += b(I) * c(I)$$
.

• pointwise multiplication
$$\mathbf{a} += \mathbf{b}(\mathbf{I}) * \mathbf{c}(\mathbf{I}).$$
 • dot product; could be sparse
$$\left(a = \sum_i b_i * c_i\right)$$

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$$\mathbf{a}(\mathbf{I},\mathbf{K}) += \mathbf{b}(\mathbf{I},\mathbf{J}) * \mathbf{c}(\mathbf{J},\mathbf{K}). \qquad \left(a_{i,k} = \sum_{i} b_{i,j} * c_{j,k}\right)$$

- matrix multiplication; could be sparse
- J is free on the right-hand side, so we sum over it

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$$\textbf{a (I,K)} \quad \textbf{b (I,J)} \quad \textbf{* c (J,K)} \, . \\ \textbf{* matrix multiplication; could be sparse} \quad \left(a_{i,k} = \sum_{j} b_{i,j} * c_{j,k}\right)$$

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Prolog has Horn clauses:

```
a(I,K) :- b(I,J) , c(J,K).
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Allow nested terms
Syntactic sugar for lists, etc.
Turing-complete

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Allow nested terms
Syntactic sugar for lists, etc.
Turing-complete

Unlike Prolog:

Terms can have values
Terms are evaluated in place
Not just backtracking!

```
distance(X) min= edge(X, Y) + distance(Y).
distance(start) min= 0.
path length := distance(end).
edge("a", "b") = 10.
edge("b", "c") = 2.
edge("c", "d") = 7.
edge("d", "b") = 1.
start = "a".
end = "d".
```

```
distance(X) min= edge(X, Y) + distance(Y).

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path_length := distance(end).

\operatorname{distance}(x) = \min_{y \in \operatorname{edge}(x,y)} \operatorname{edge}(x,y) + \operatorname{distance}(y)
\operatorname{distance}(\operatorname{Start}) = 0
\operatorname{Path} \operatorname{length} = \operatorname{distance}(\operatorname{End})
```

Variables not present in the head of an expression are aggregated over like with the dot product example.

```
\min_{y \in \text{edges}(x, \cdot)} \text{edge}(x, y) + \text{distance}(y)
\text{tance}(\text{End})
```

```
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distance(start) min= 0
path_length
                                   nce(end).
          \operatorname{distance}(x) = \min_{y \in \operatorname{edges}(x, \cdot)}
                                            Here the "min="
                                             aggregator only
      distance(Start) = 0
                                                keeps the
          Path length = distance(End)
                                              minimal value
                                              that we have
                                               computed
```

Note: Aggregation was already present in our mathematical definition.

Shortest path

Path length = distance(End)

```
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```

After this converges we can *query* the state of the Dyna program.

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? path_length

Length at the end

After this converges we can *query* the state of the Dyna program.

```
? path_length
```

? distance("c") ~

The distance of some other vertex

After this converges we can *query* the state of the Dyna program.

```
? path_length
? distance("c")
? distance(X)
All of the
vertices
```

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```

After this converges we can *query* the state of the Dyna program.

```
? path_length
? distance("c")
? distance(X)
? distance(X) > 7
```

All the vertices more than 7 away

```
distance(X)     min= edge(X, Y) + distance(Y).
distance(start) min= 0.
path_length     := distance(end).
```

After this converges we can *query* the state of the Dyna program.

```
? path_length
? distance("c")
? distance(X)
? distance(X) > 7
? edge("a",X)
```

All of the edges leaving "a"

Aggregators

Associative/commutative:

```
b += a(X). % number
c max= a(X).
q |= p(X). % boolean
r &= p(X).
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• Last one wins:

- fly(X) := true if bird(X).
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- fly(bigbird) := false.

Associative/commutative: Choose any value:

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- e ?= c.
- User definable aggregators
 - a(X) **smiles**= b(X, Z).

Associative/commutative:

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.

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$$=$$
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$$\&=$$
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- User definable aggregators
 - a(X) smiles= b(X, Z).
 - (Just define all of the operation of an commutative semigroup)

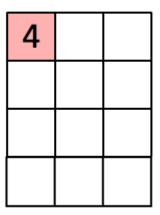
1 _{×1}	1,0	1,	0	0
0,0	1,	1,0	1	0
0 _{×1}	0,×0	1,	1	1
0	0	1	1	0
0	1	1	0	0
0	0	1	1	0

Input image

4	

Convolution output

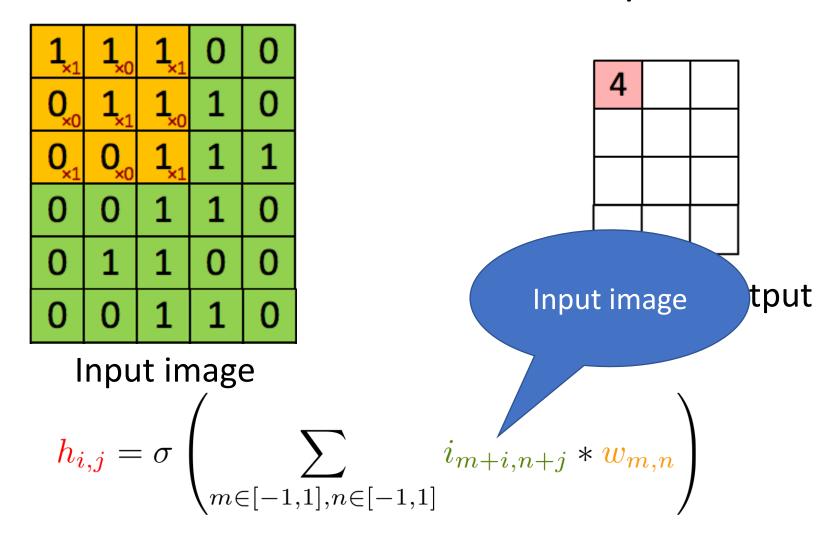
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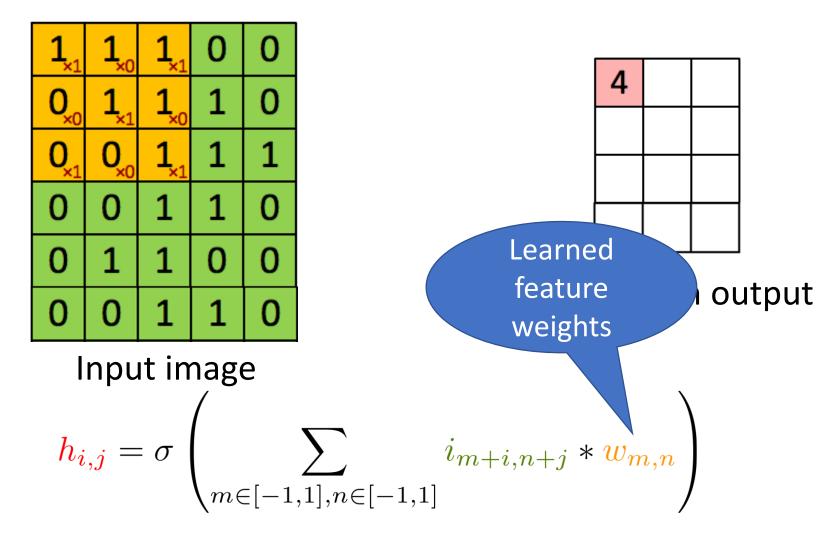


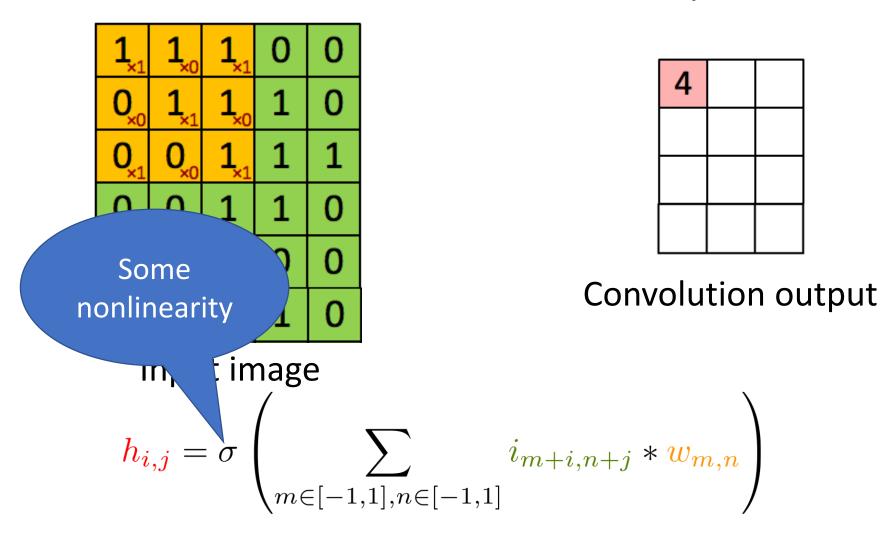
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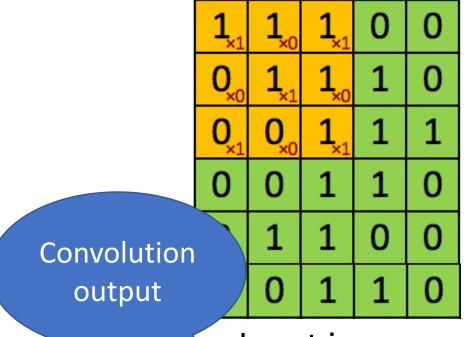
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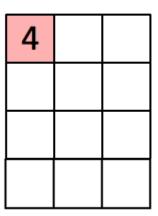
$$egin{align} h_{i,j} &= \sigma \left(\sum_{m \in [-1,1], n \in [-1,1]} i_{m+i,n+j} * w_{m,n}
ight) \end{split}$$











Convolution output

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```
(activation(I, J)).
(X) := 1 / (1 + exp(-X)).
```

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\sigma\sigma(X) := 1 / (1 + \exp(-X)).
= \sigma(\operatorname{activation}(I, J)).
\operatorname{activation}(I, J) += \operatorname{input}(I + M, J + N) * \operatorname{weight}(M, N).
\operatorname{weight}(DX,DY) := \operatorname{random}(*,-1,1) \text{ for } DX:-1..1, DY:-1..1.
```

$$h_{i,j} = \sigma \left(\sum_{m \in [-1,1], n \in [-1,1]} i_{m+i,n+j} * w_{m,n} \right)$$

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$$= \sigma(\operatorname{activation}(I, J)).$$

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$$\operatorname{weight}(DX, DY) := \operatorname{random}(*, -1, 1) \text{ for } DX: -1..1, DY: -1..1.$$

$$h_{i,j} = \sigma \left(\sum_{m \in [-1,1], n \in [-1,1]} i_{m+i,n+j} * w_{m,n} \right)$$

```
\sigma\sigma(X) := 1 \ / \ (1 + \exp(-X)). = \sigma(\text{activation}(I, J)) activation(I, J) += \inf(I + M, J + N) * \text{weight}(M, N). weight(DX,DY) := random 1,1) for DX:-1..1, DY:-1..1.
```

Summation became an aggregator

```
h_i \qquad \text{We can easily} \\ \sigma\sigma(X) := \qquad (1 + \exp(-X)). \\ = \sigma(\text{activation}(I, J)). \\ \text{activation}(I, J) += \inf(I + M, J + N) * \text{weight}(M, N). \\ \text{weight}(DX,DY) := \text{random}(*,-1,1) \text{ for } DX:-1..1, DY:-1..1.
```

$$h_{i,j} = \sigma \left(\sum_{m \in [-1,1], n \in [-1,1]} i_{m+i,n+j} * w_{m,n} \right)$$

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```

Our ranges over m and n are reflected in the shape of weight

$$h_{i,j} = \sigma \left(\sum_{m \in [-1,1], n \in [-1,1]} i_{m+i,n+j} * w_{m,n} \right)$$

Here keys are integers but we can also support more complicated structures

```
\sigma(X) = 1 / (1 + \exp(-X)).

out(J) = \sigma(activation(J)).

activation(J) += out(I) * edge(I,J).
```

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```

All weights have been rolled into the edges connecting neurons

```
\sigma(X) = 1 / (1 + \exp(-X)).
out(J) = \sigma(\arctan(J)).
activa ion(J) += out(I) * edge(I,J).
```

The output of a neuron is our nonlinearity applied to the sum of its inputs

```
\sigma(X) = 1 / (1 + \exp(-X)).
out(J) = \sigma(\text{activation}(J)).
activation(J) += out(I) * edge(I,J).
```

Note: nowhere in this program do we specify the form of our variables I, J

```
\sigma(X) = 1 / (1 + \exp(-X)).

out(J) = \sigma(activation(J)).

activation(J) += out(I) * edge(I,J).
```

Instead we can specify the structure of keys inside the definition of edge.

```
edge(input(X,Y),hidden(X+DX,Y+DY)) = weight(DX,DY).
weight(DX,DY) := random(*,-1,1) for DX:-1..1, DY:-1..1.
```

```
\sigma(X) = 1 / (1 + \exp(-X)).

out(J) = \sigma(activation(J)).

activation(J) += out(I) * edge(I,J).
```

```
edge(input(X,Y),hidden(X+DX,Y+DY)) = weight(DX,DY).
weight(DX,DY) := random(*,-1,1) for DX:-1..1, DY -1..1.
```

The weight do not depend on the absolute location of the input, so this is a convolution again.

• Gibbs, MCMC – flip variable, compute likelihood ratio, accept or reject

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- Iterative algorithms loopy belief propagation, numerical optimization

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- Implementations and more in:
 - Dyna: Extending Datalog for modern AI. (Eisner & Filardo 2011)
 - Dyna: A non-probabilistic language for probabilistic AI. (Eisner 2009)

How much can a declarative language save us?

Implementing shortest path

Implementing shortest path

Dyna (Declarative)

Implementing shortest path

Dyna (Declarative)

```
distance(X) min= edge(X, Y)
               + distance(Y).
distance(start) min= 0.
path length = distance(end).
```

Java (Procedural)

```
queue = new FifoQueue<Pair<String, Float>>();
distances = new HashMap<String, Float>();
edges = new HashMap<Pair<String, String>,Float>();
// load edges
queue.push("start");
while(!queue.empty()) {
  d = queue.pop();
 for(e : edge) {
    if(e.first().second().equals(d.first())) {
      if(distance.get(e.first()) <</pre>
         d.second() + e.second()) {
        distance.put(e.first(),
                     d.second() + e.second());
        queue.push(e.first());
path length = distances.get("end");
```

Dyna (Declarative)

```
queue = new <a href="mailto:priorityQueue">PriorityQueue</a> <a href="mailto:String">String</a>, Float>();
distances = new HashMap<String, Float>();
edges = new HashMap<Pair<String, String>,Float>();
// load edges
queue.push("start", 0);
while(!queue.empty()) {
  d = queue.pop();
  for(e : edge) {
    if(e.first().second().equals(d.first())) {
       n = d.second() + e.second();
       if(distance.get(e.first()) < n) {</pre>
         distance.put(e.first(), n);
         queue.push(e.first(), n);
path_length = distances.get("end");
```

Dyna (Declarative)

```
queue = new PriorityQueue<String, Float>();
distances = new HashMap<String, Float>();
edges = new HashMap<String,Map<String,Float>>();
// load edges
queue.push("start", 0);
while(!queue.empty()) {
  d = queue.pop();
 for(e : edge.get(d.first())) {
    n = d.second() + e.second();
    if(distance.get(e.first()) < n) {</pre>
      distance.put(e.first(), n);
      queue.push(e.first(), n);
path length = distances.get("end");
```

Dyna (Declarative)

```
placeIndex = new HashMap<String,Integer>();
queue = new PriorityQueue<Integer, Float>();
distances = new float[num places];
edges = new float[num places][num places];
// load edges
queue.push(placesIndex.get("start"), 0);
while(!queue.empty()) {
  d = queue.pop();
  1 = edges[d.first()];
  for(j = 0; j < 1.length; j++) {
    n = d.second() + 1[j];
    if(distances[j] < n) {</pre>
      distances[j] = n;
      queue.push(j, n);
path length = distances[placeIndex.get("end")];
```

Dyna (Declarative)

```
placeIndex = new HashMap<String,Integer>();
edges = new float[num places][num places];
// load edges
float distance(from) {
  if(from == placeIndex.get("start")) {
    return 0;
  1 = edges[from];
  r = infinity;
  for(j = 0; j < 1.length; j++) {
    n = \frac{distance(j)}{distance(j)} + l[j];
    if(n < r)
      r = n;
  return r;
path length = distance(placeIndex.get("end"));
```

path

Dyna (Declarative)

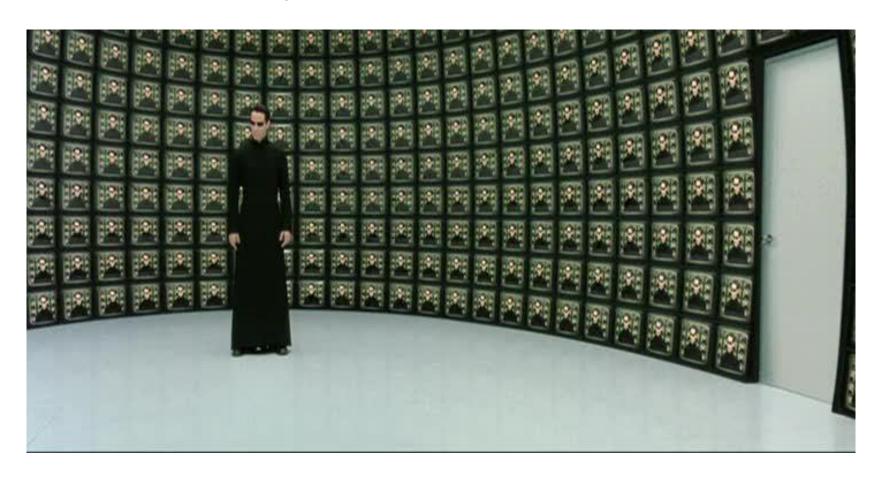
Java (Procedural)

```
placeIndex = new // load float A single Dyna program can represent hundreds of possible implementations.
```

Other implementations
(not shown here) include A*
and bidirectional search, and
choice of data structures to
support dynamic graphs

Given all of these implementations,

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- Take the Architect's deal
 - Restart the Matrix
 - Let all the humans in Zion die
 - But restart Zion with 16 females and 7 males (fight another day)

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 - Save Trinity

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- Follow "an emotion specifically designed to overwhelm logic & reason"
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 - YOLO, figure this out as we go (unknown reward)

This raises the next question ...

This raises the next question ... can machines love

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or at least make irrational choices

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 $action = \operatorname{argmax} \pi(\cdot | \dots)$

The "Rational" Choice



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Exploitation

$$action \sim \pi(\cdot|\ldots)$$

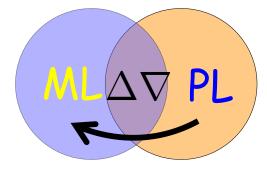
The "Irrational" Choice (Randomly sample)



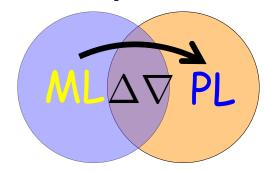
Exploration

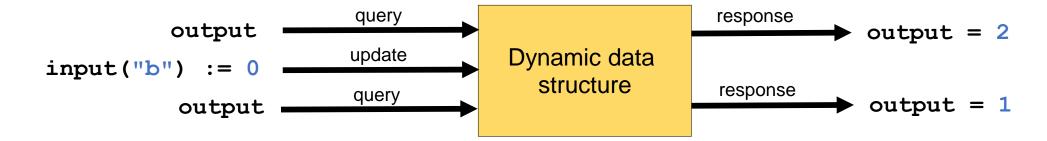
Outline

- Why Declarative Programming?
- Quick introduction to the Dyna language



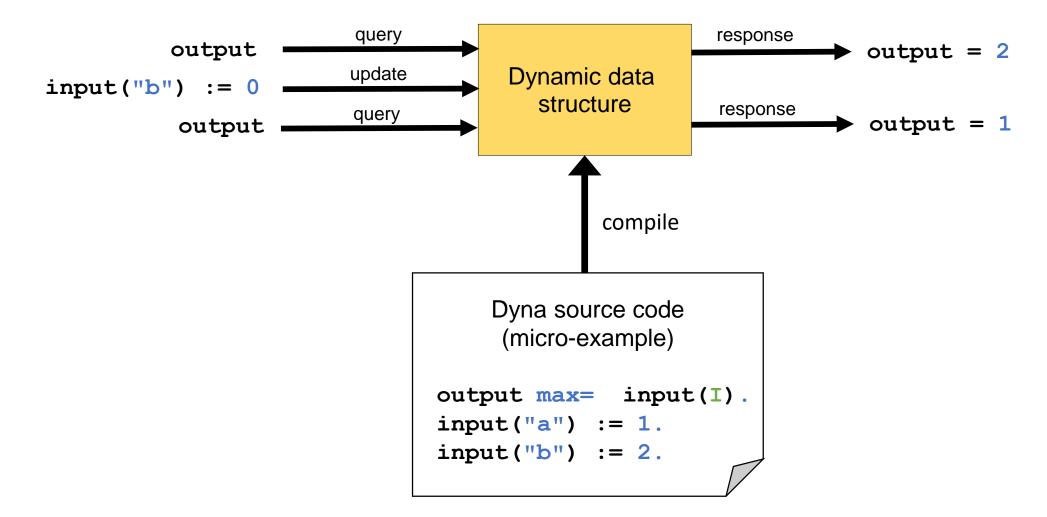
Automatic optimization of Dyna programs

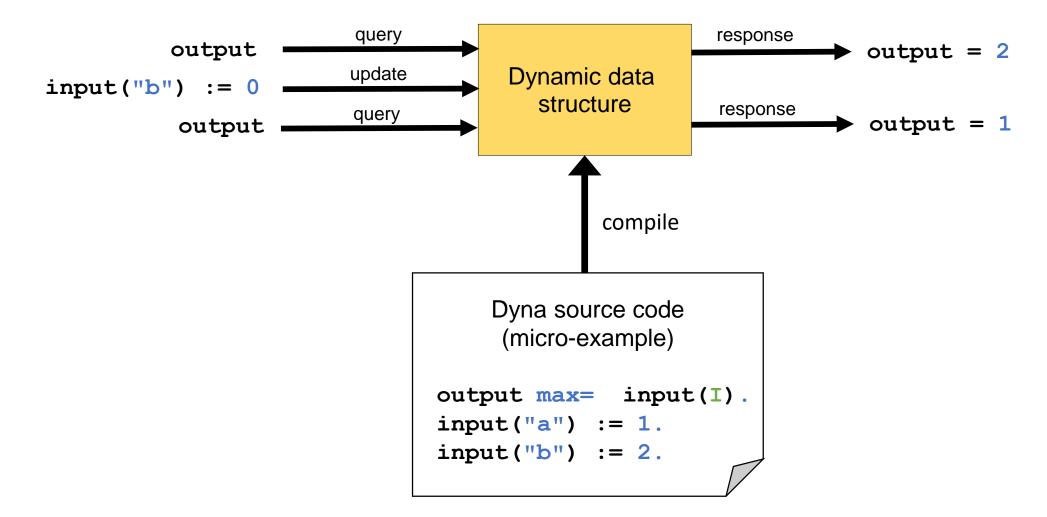


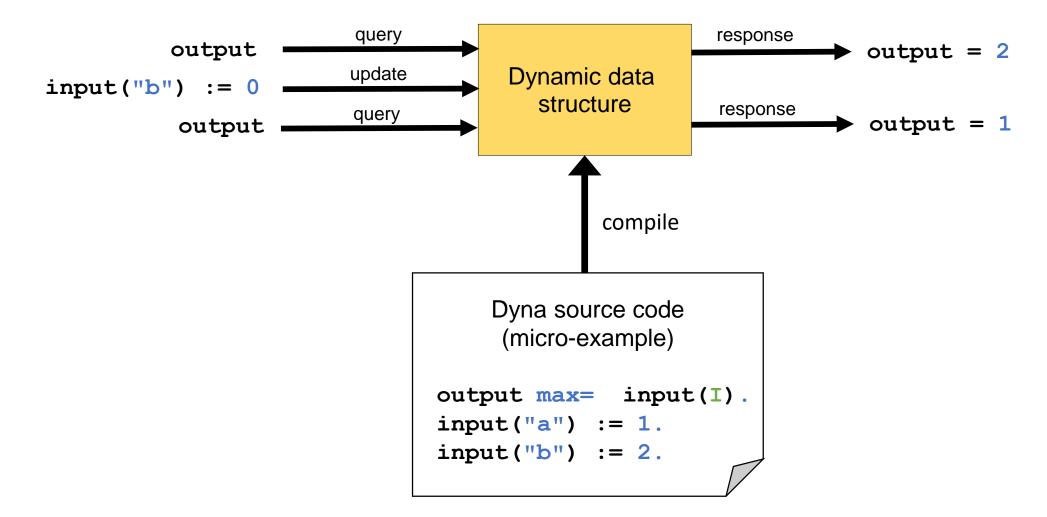


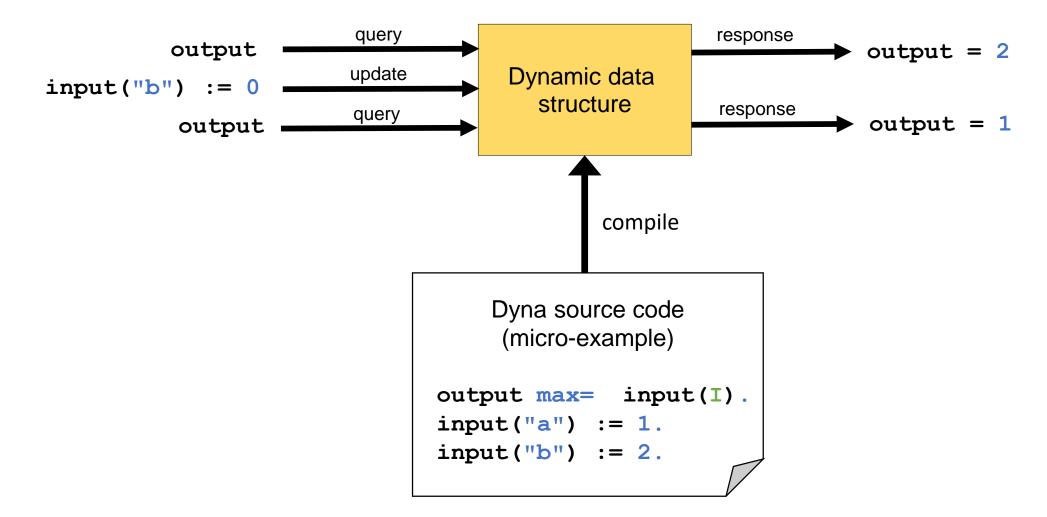
```
Dyna source code
  (micro-example)

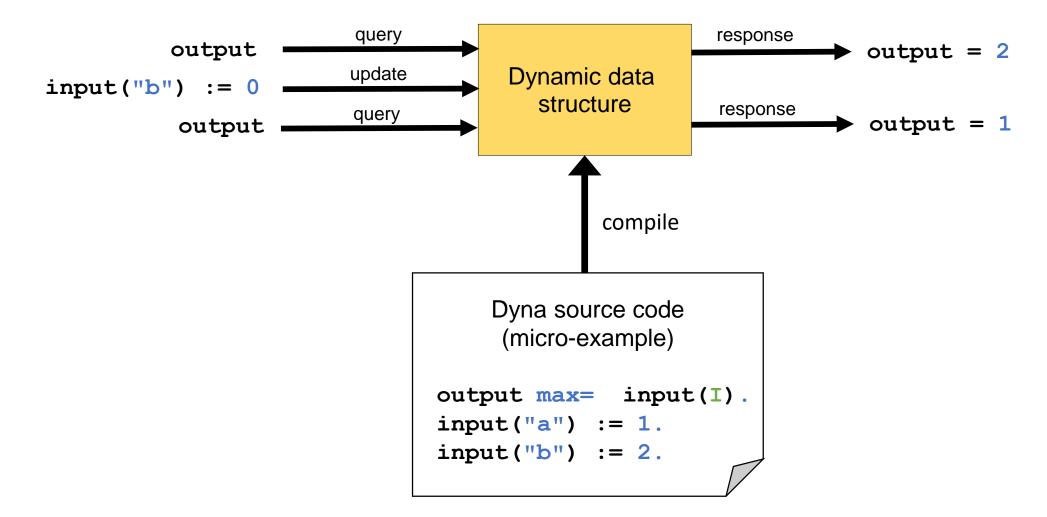
output max= input(I).
input("a") := 1.
input("b") := 2.
```

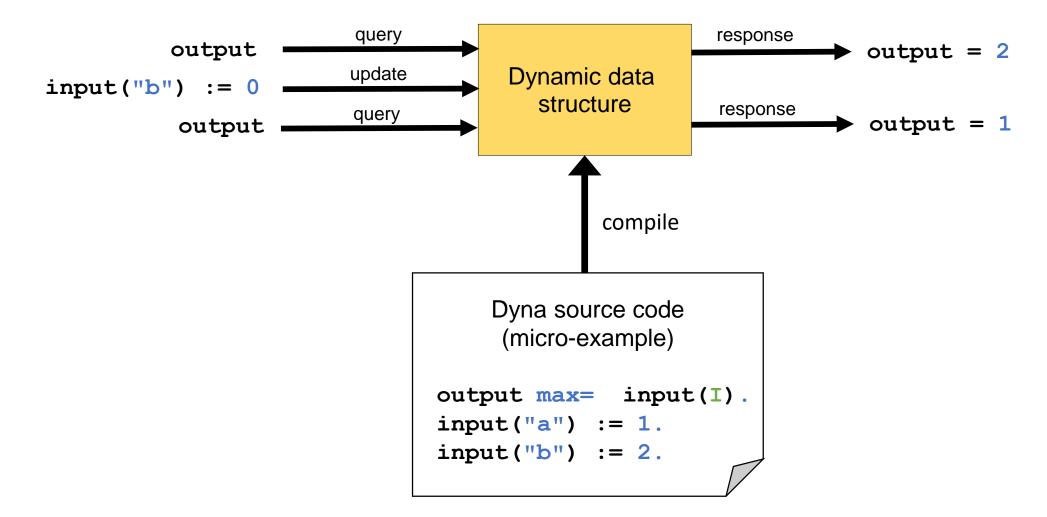


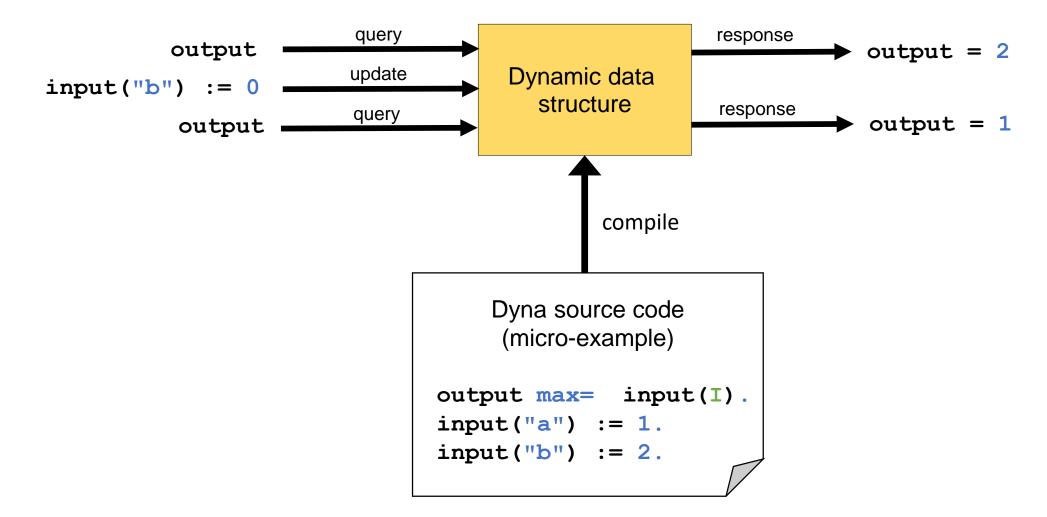


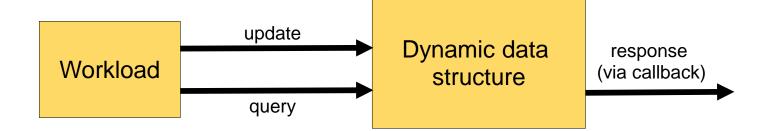


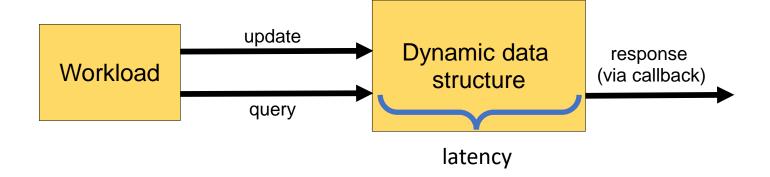


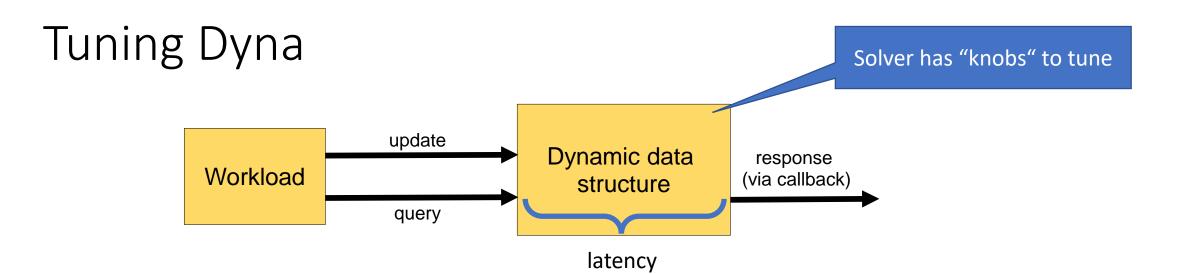




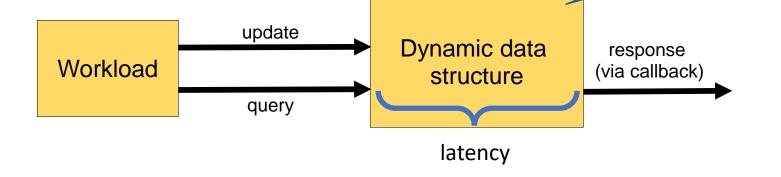






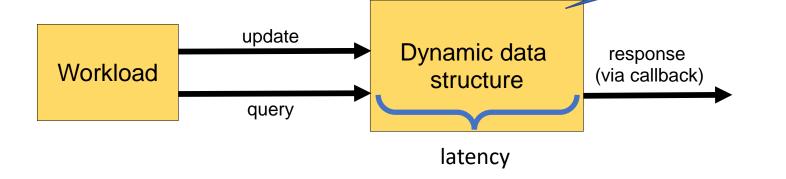


Solver has "knobs" to tune





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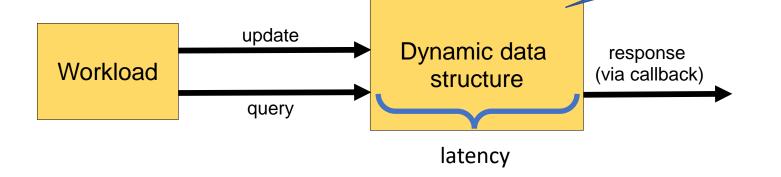


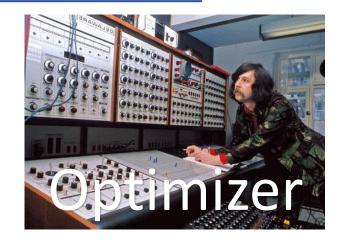
Example knob: eager or lazy updates? e.g., **dynamic max data structure**

```
% Dyna:
output max= input(I).
```

- *O*(*log n*) per update
- *O(n)* per batch update ("heapify")

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$$\rho(\pi) = \mathbb{E}\left[\sum_{i=1}^{\infty} \gamma^i \lambda_i \operatorname{latency}(i)\right]$$

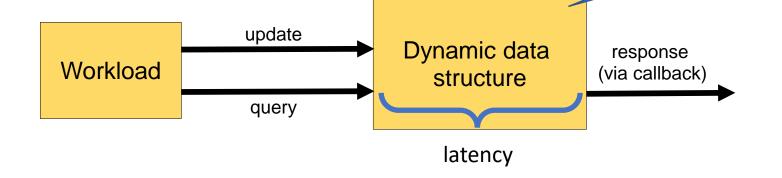
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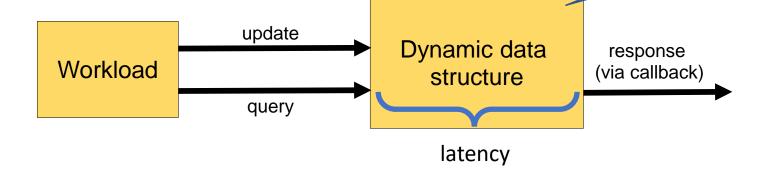
knob settings

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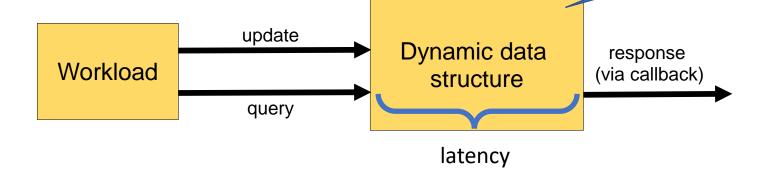
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Tuning Dyna

Solver has "knobs" to tune





Total cost knob setting

Average latency on workload

Encourage earlier jobs to finish first

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knob settings

Example knob: eager or lazy updates? e.g., **dynamic max data structure**

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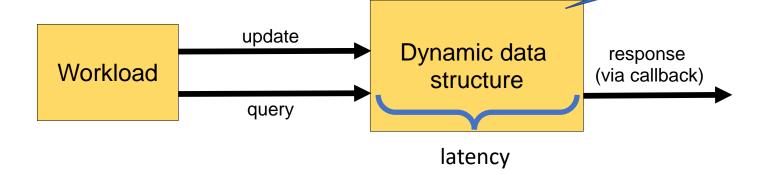
output max= input(I).

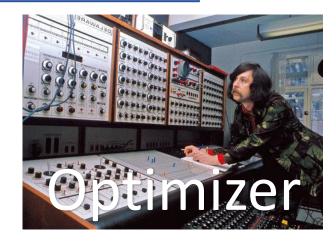
Max-heap:

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Total cost knob setting Average latency on workload

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urgency

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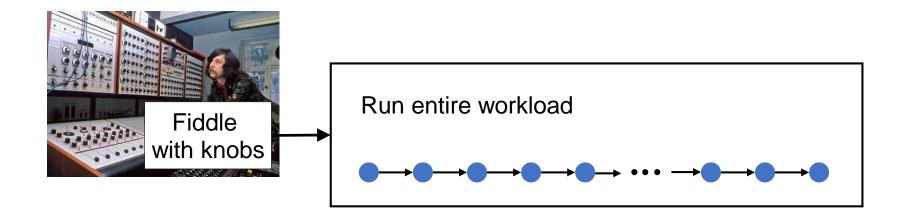
% Dyna:

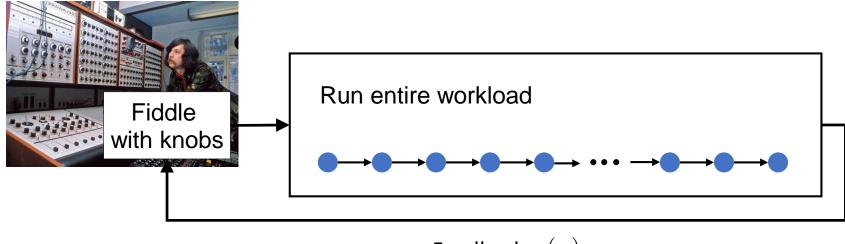
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Max-heap:

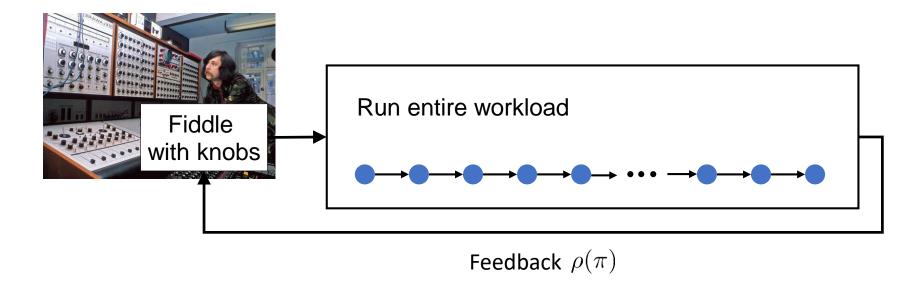
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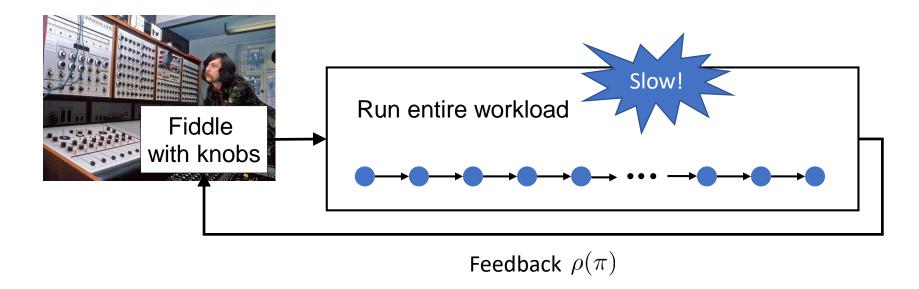




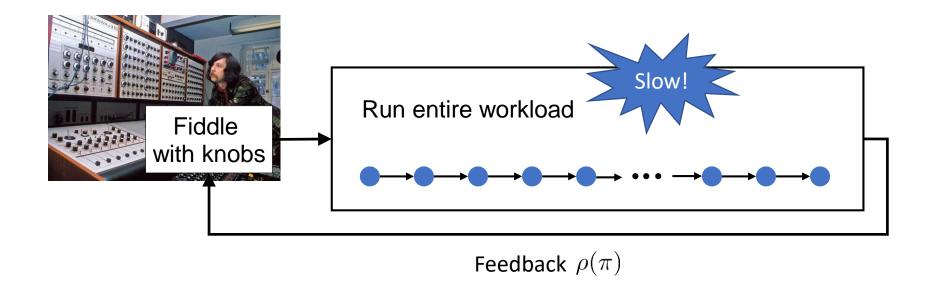
Feedback $\rho(\pi)$



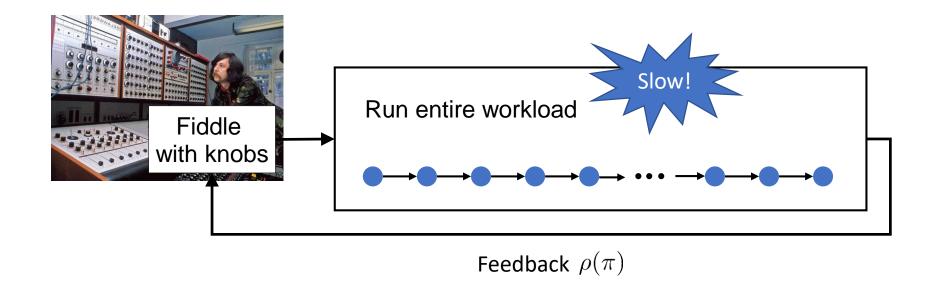
• Reasonable way to tune knobs off-line (used by PhiPac, ATLAS, SATZilla)



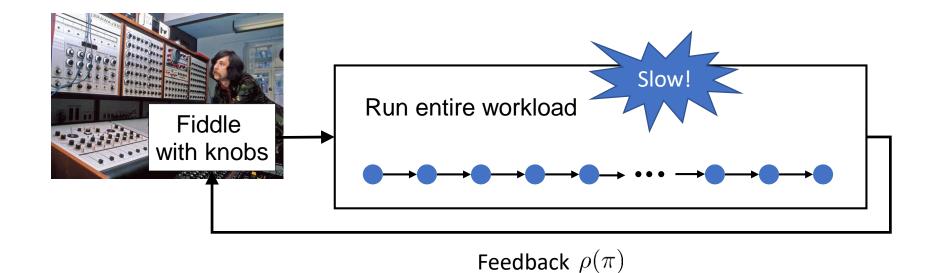
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- How do we tighten the loop to get feedback more often?

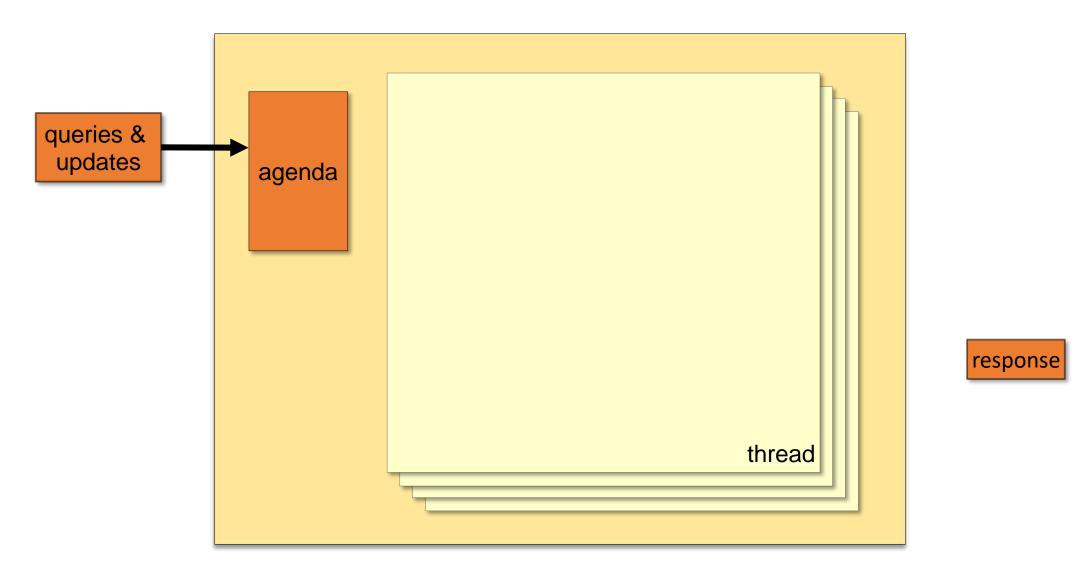


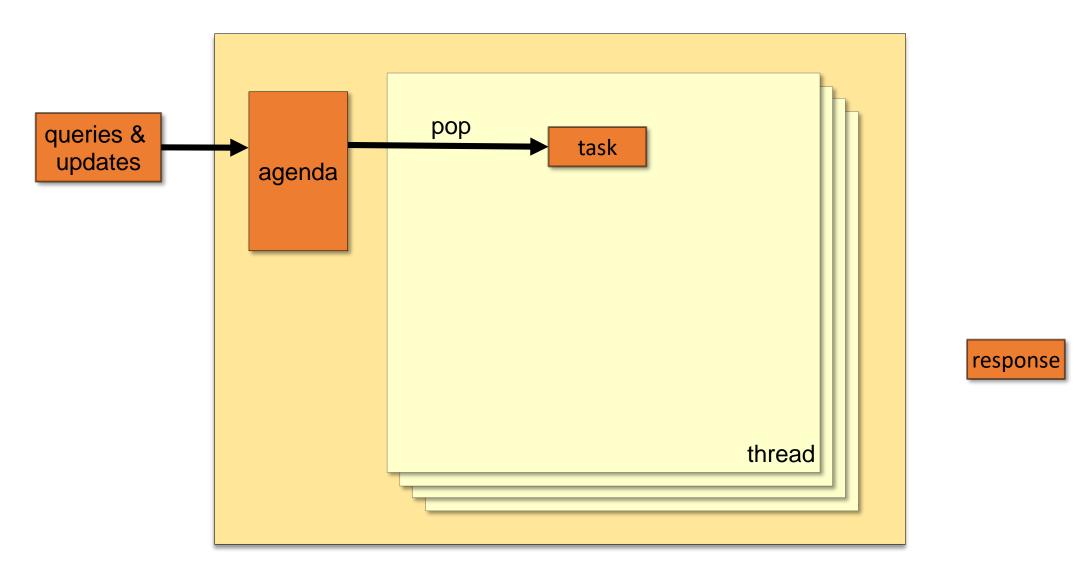
Open up the solver

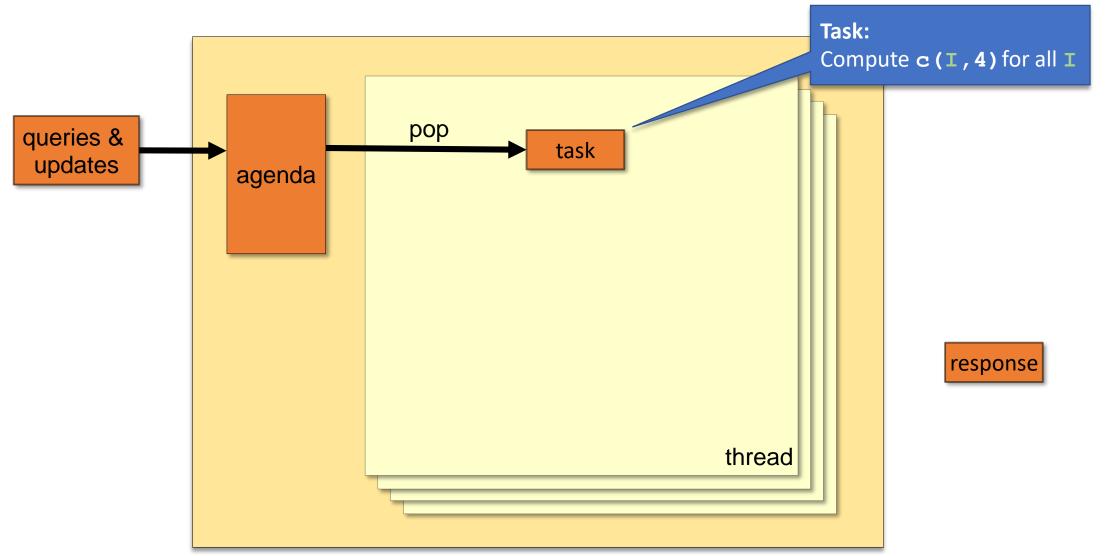
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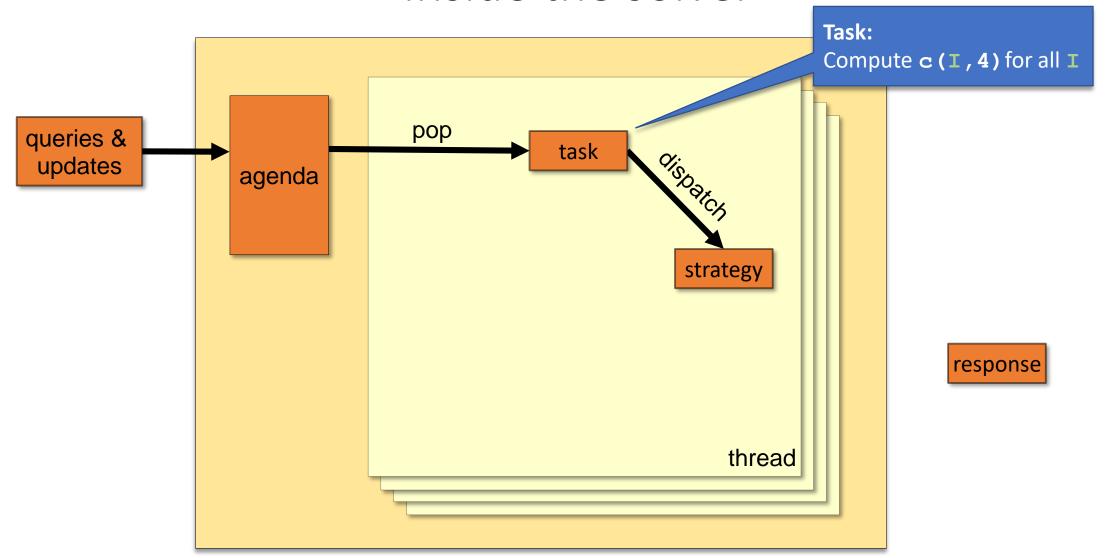
queries & updates response

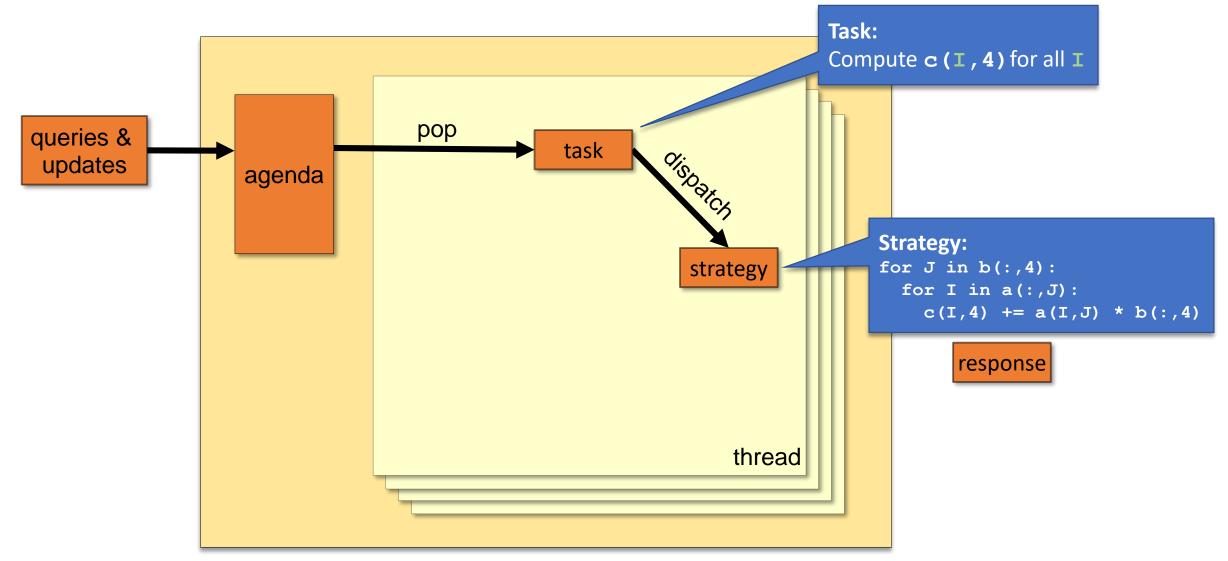


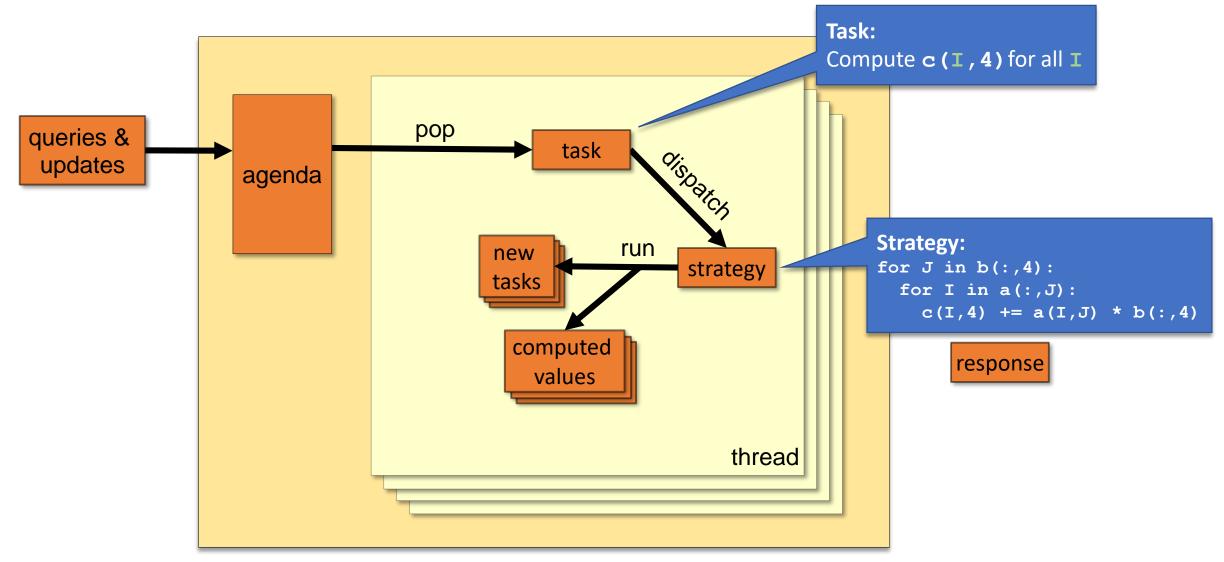


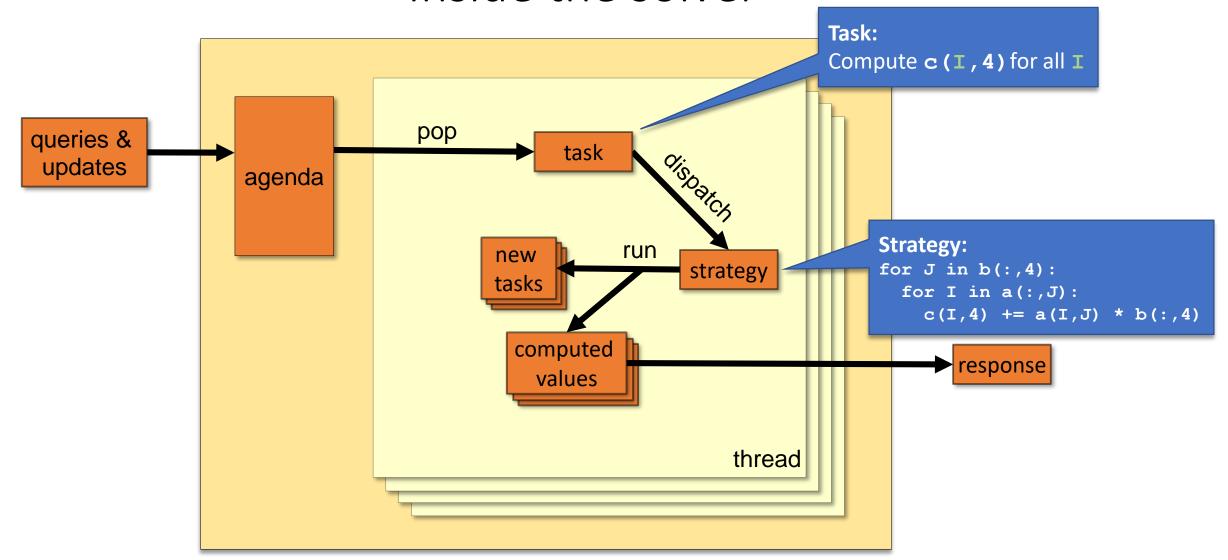


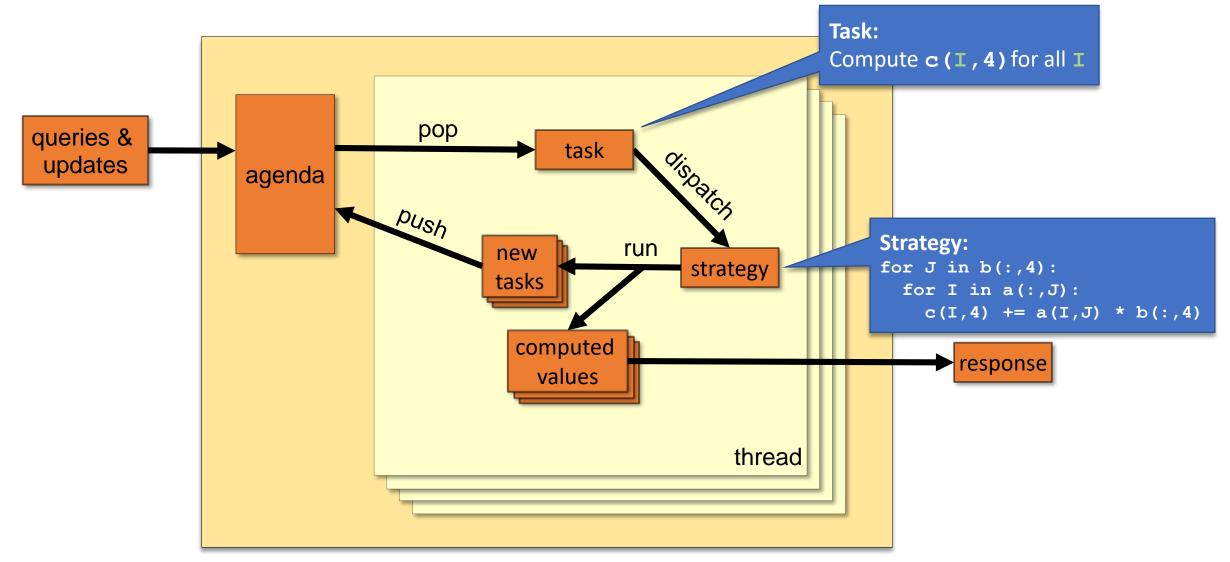








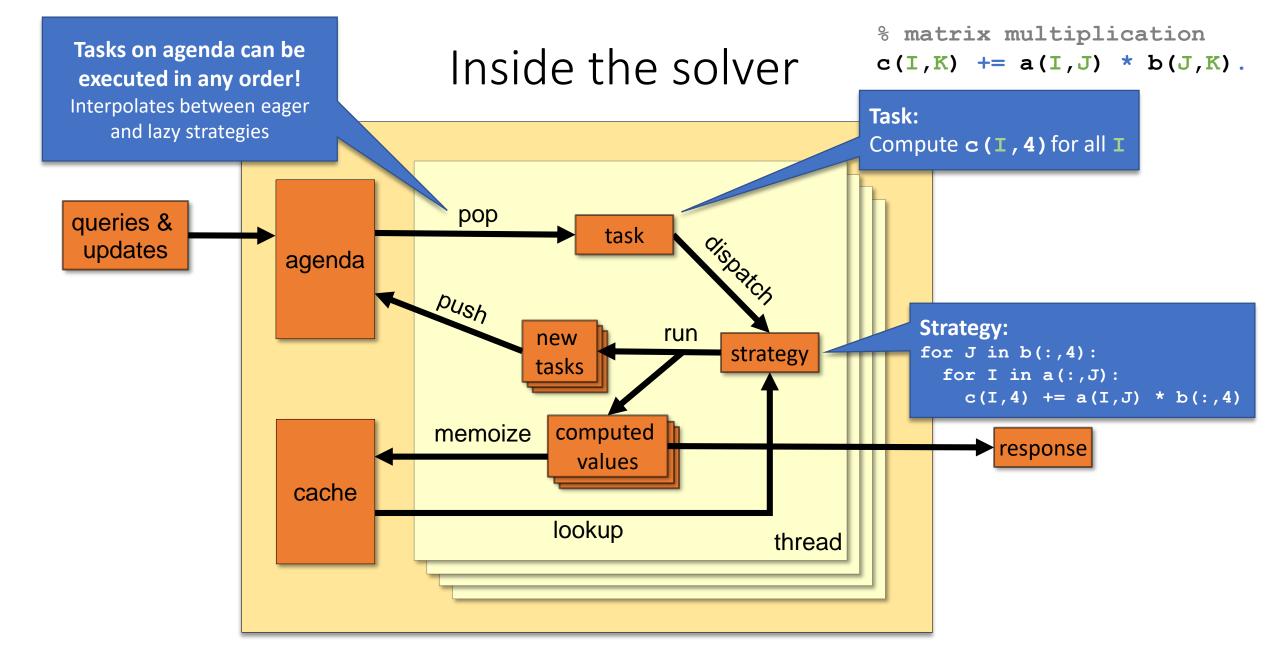


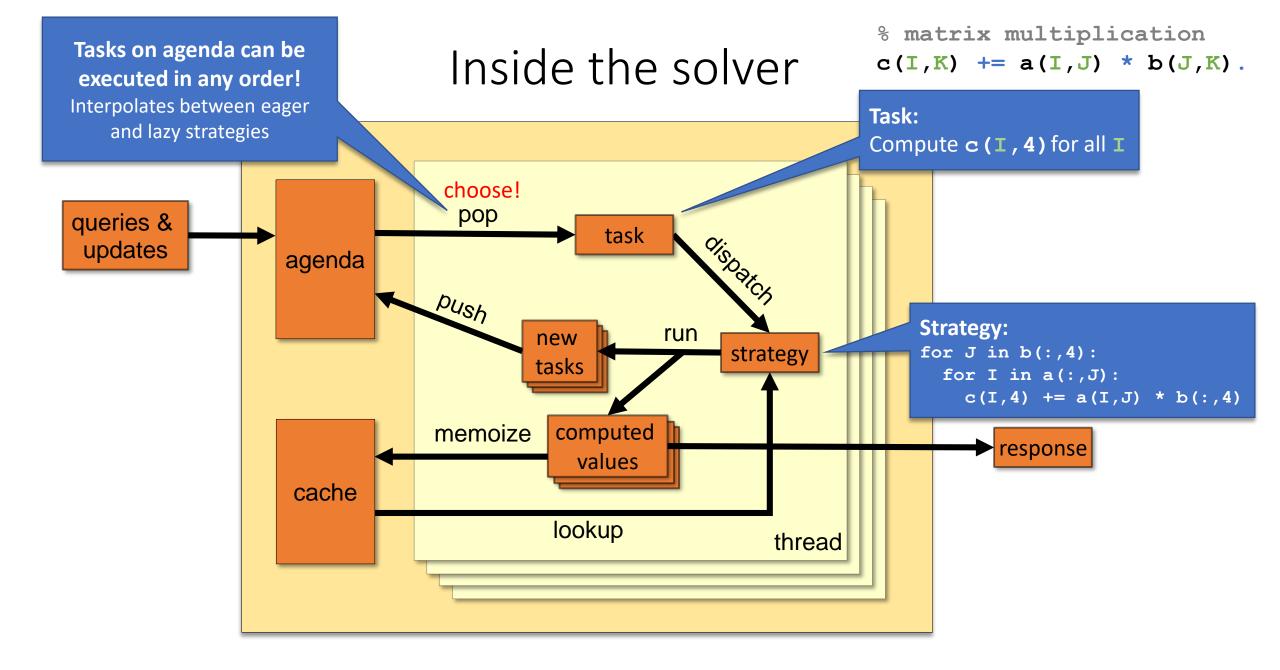


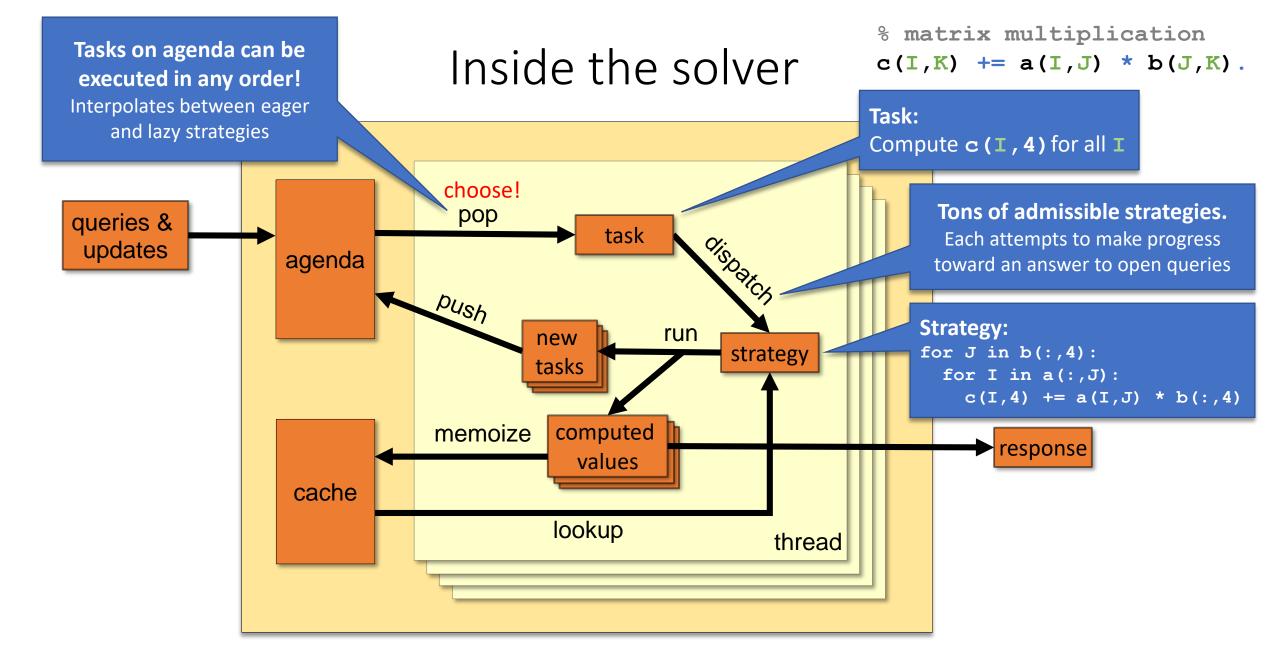
% matrix multiplication Inside the solver c(I,K) += a(I,J) * b(J,K).Task: Compute c (I, 4) for all I pop queries & task updates agenda Push Strategy: run new strategy for J in b(:,4): tasks for I in a(:,J): c(I,4) += a(I,J) * b(:,4)computed memoize response values cache

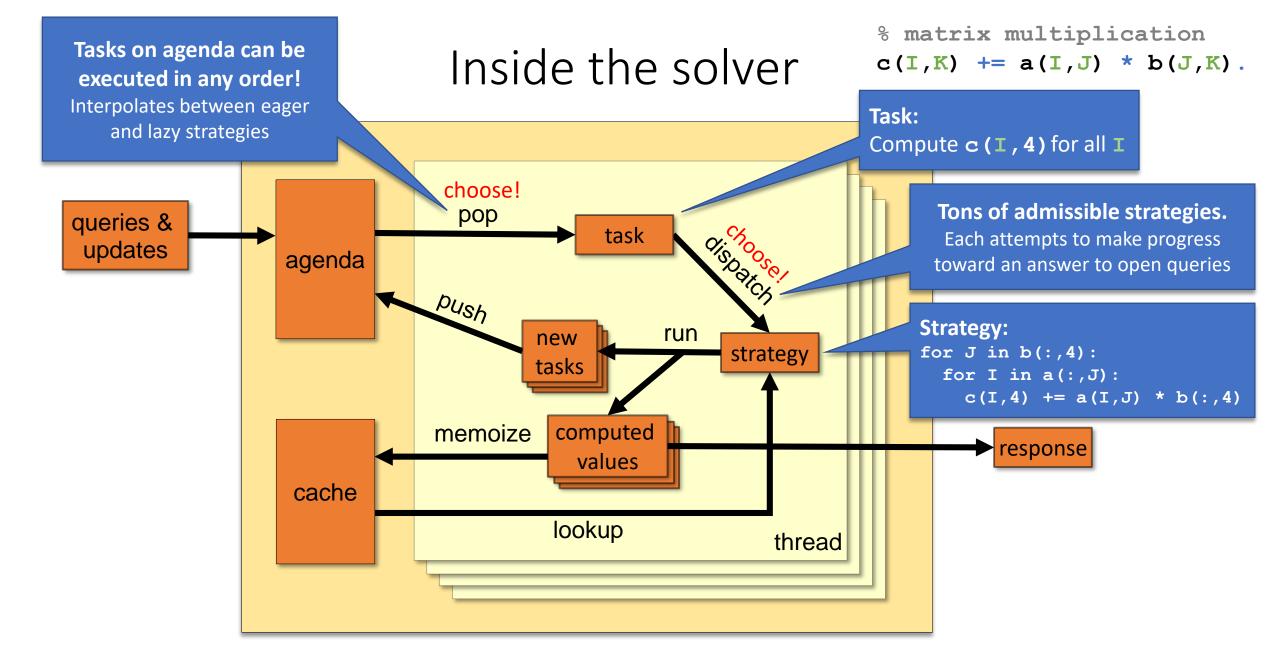
thread

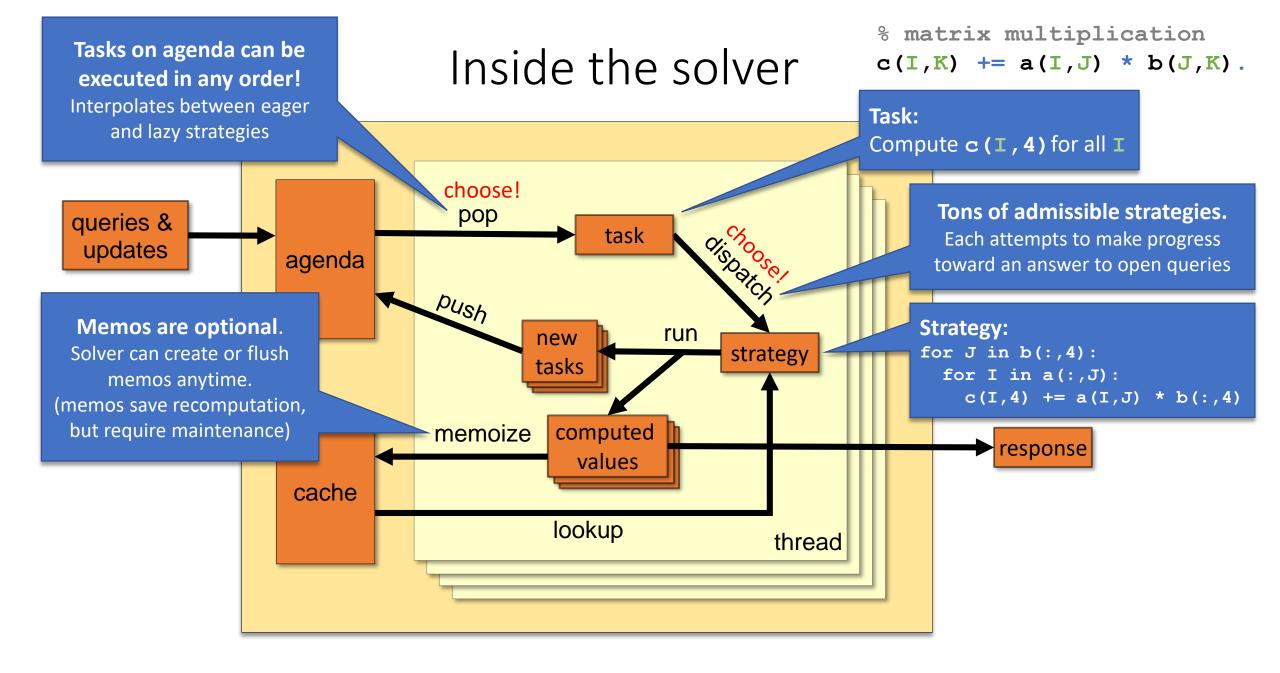
lookup

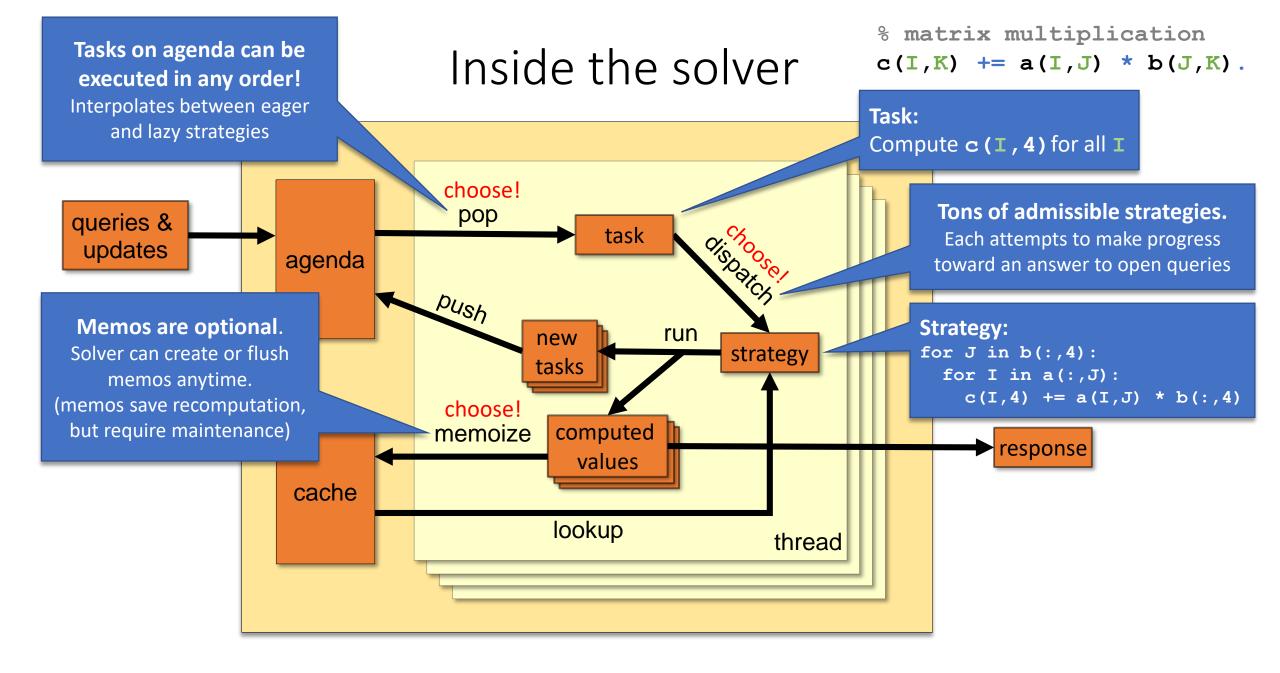












Solver should systematize all the reasonable implementation tricks that programmers might use and make them work together correctly.

Parallelizing independent computations

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- Ordering dependent computations

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 - Memoization policy; choose low-level data structures

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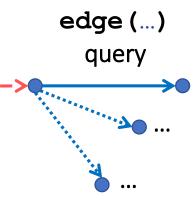
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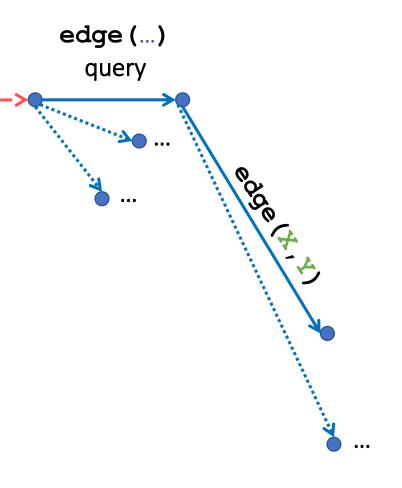
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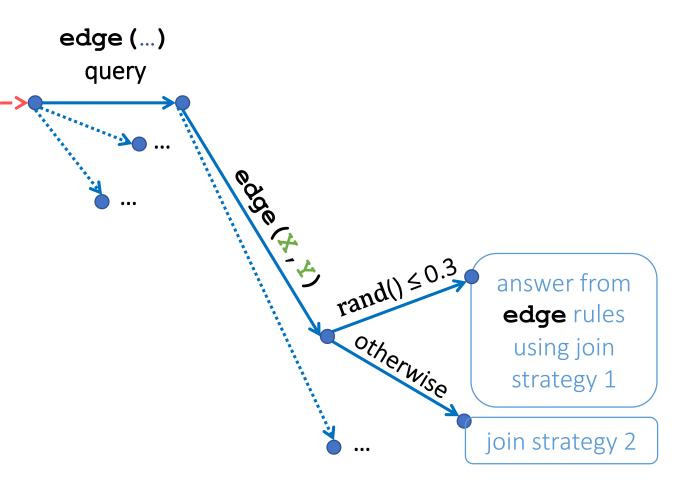
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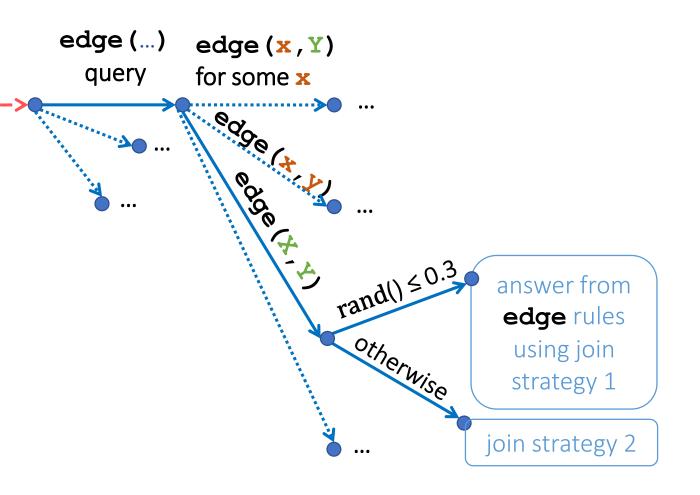


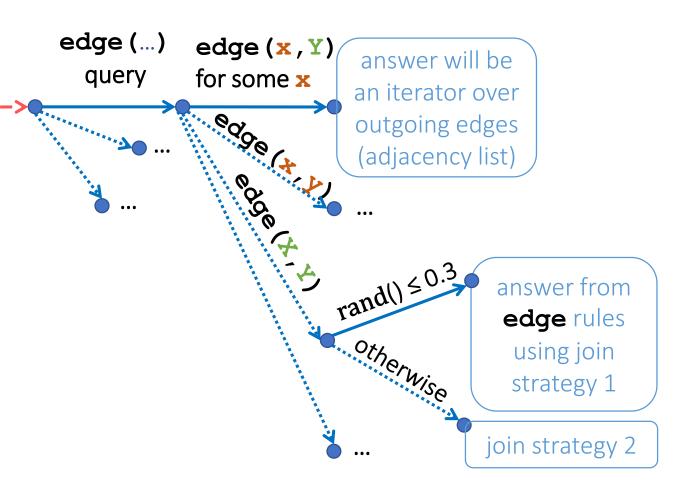
```
edge (...)
query
```

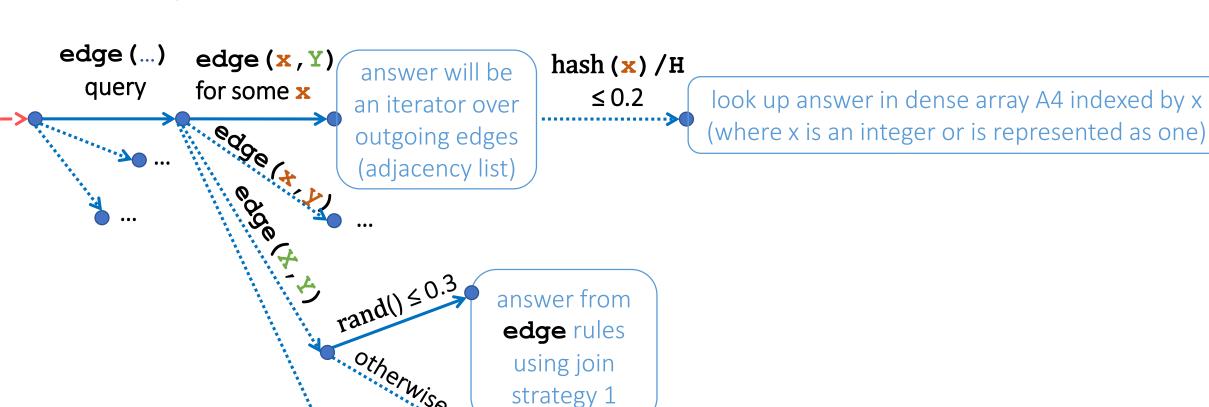




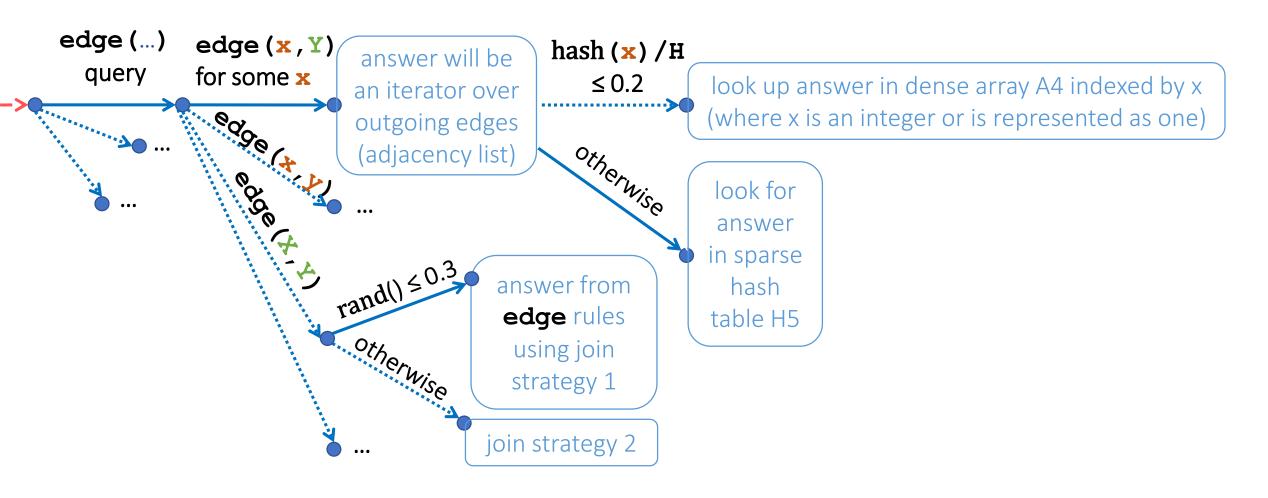


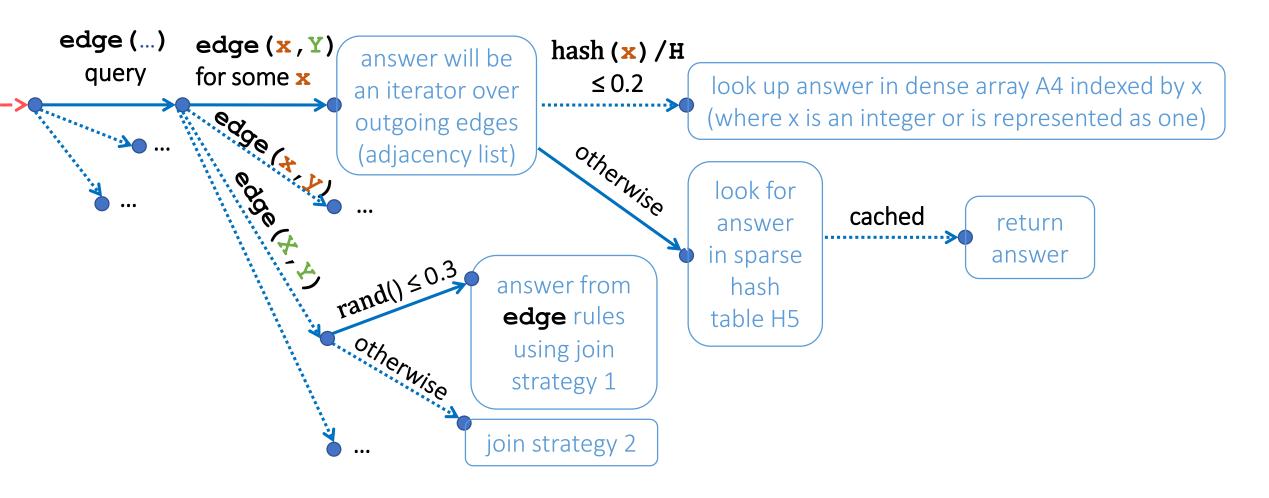


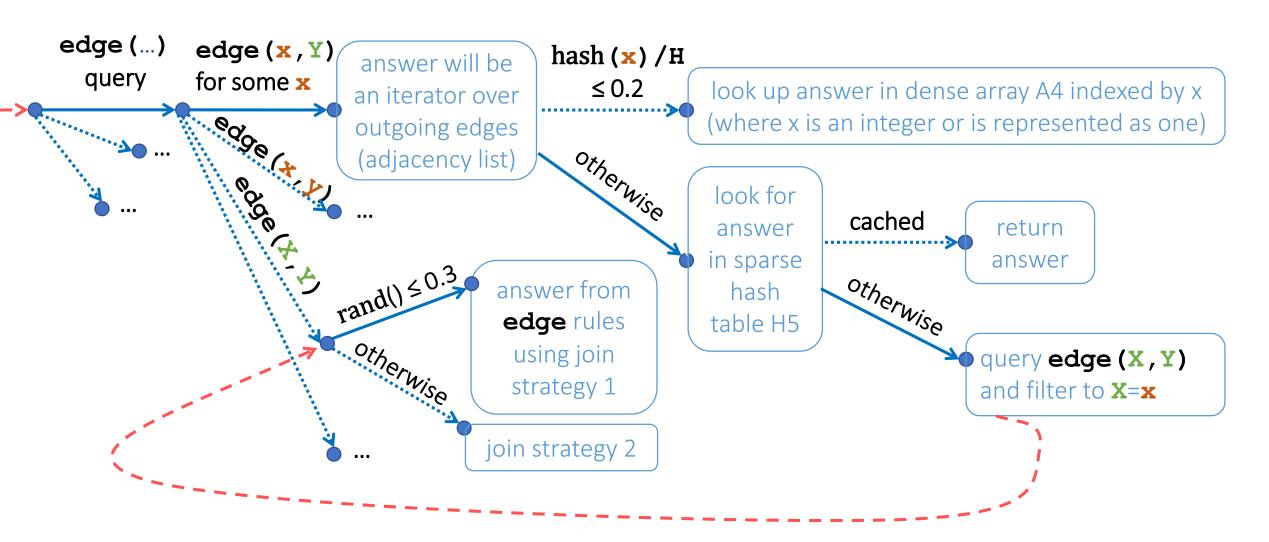


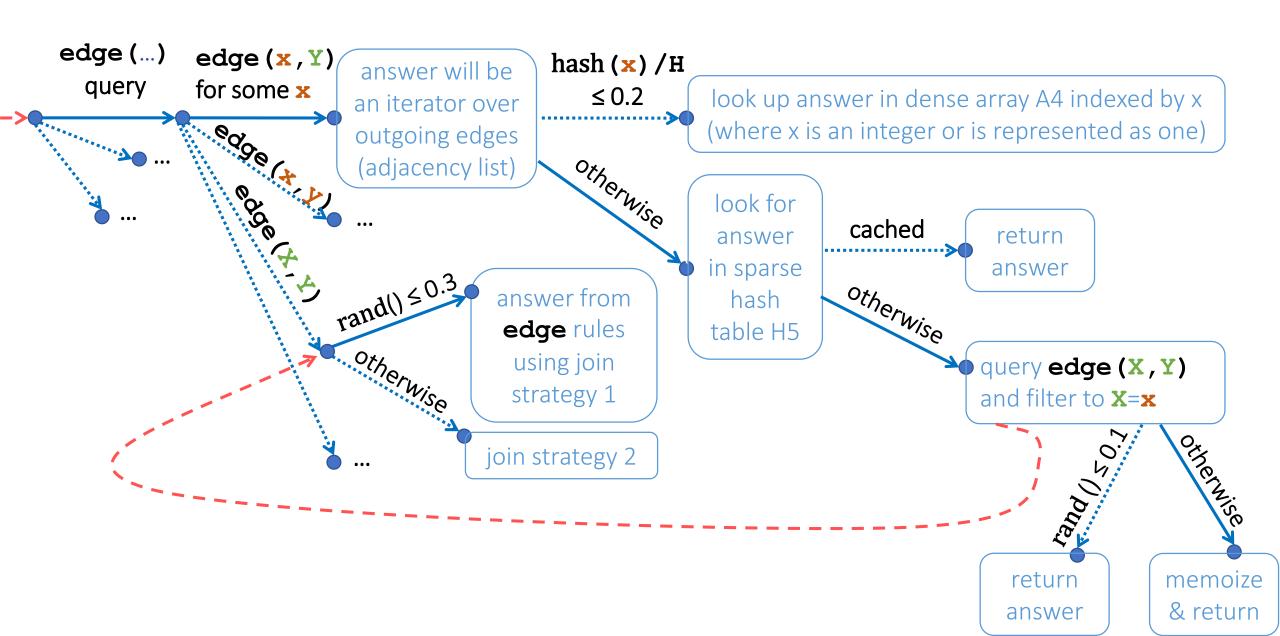


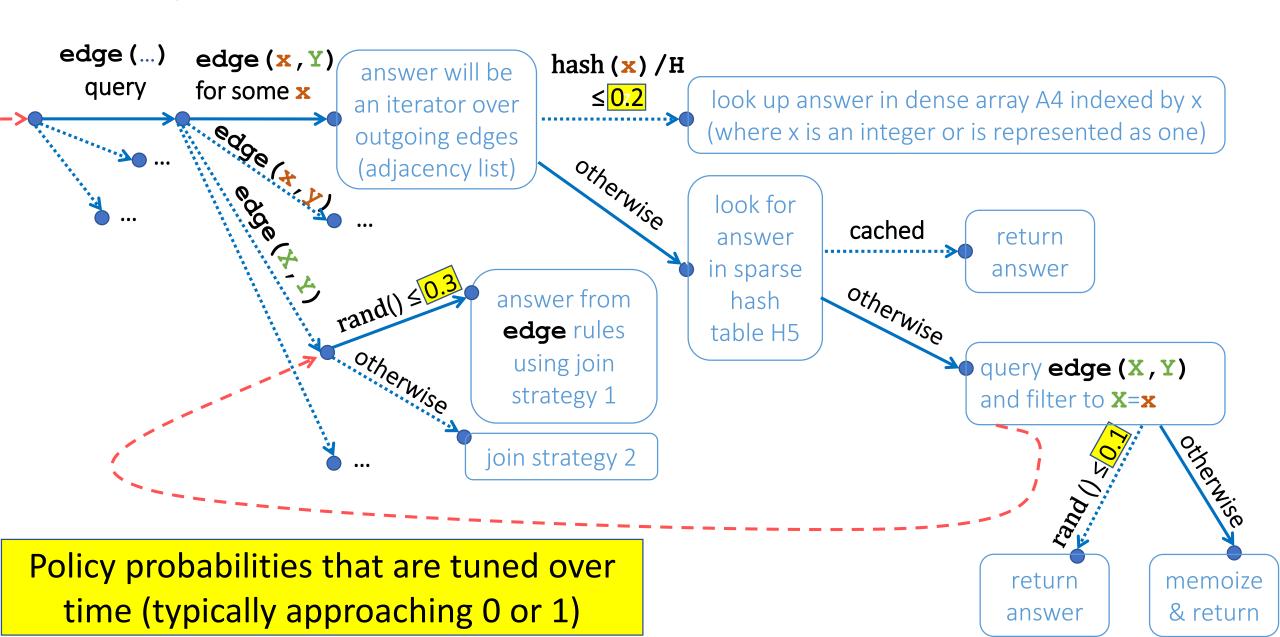
join strategy 2











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Agenda characteristics

- Are there a lot of open queries?
- What's on the agenda? How long has it been there?

Stochastically conditioned on the following information (features).

Task characteristics

- What type of task?
- What are the task parameters?
- Who requested the task?

Dataflow

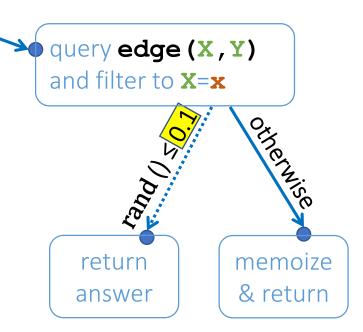
- What depends on this task (children)?
- What does this task depend on (parents)?

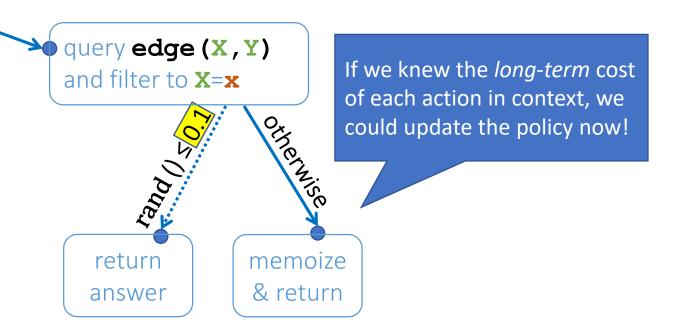
Agenda characteristics

- Are there a lot of open queries?
- What's on the agenda? How long has it been there?

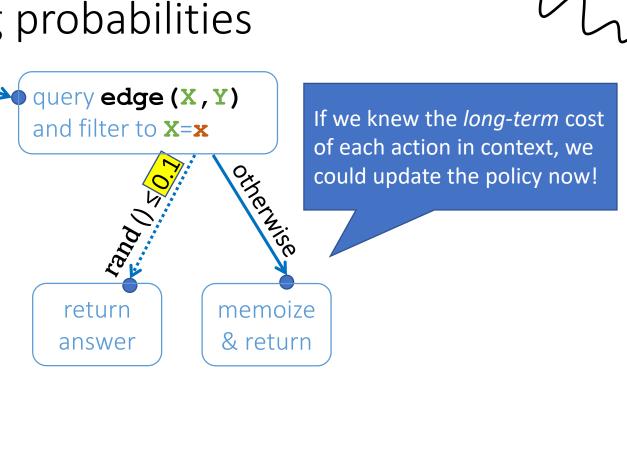
Cache characteristics

- Statistics: number, hit rate, frequency, & recency of memos (broken down by type)





Tuning probabilities query edge (X,Y) If we knew the *long-term* cost and filter to X=x of each action in context, we could update the policy now! a_1 a_2 memoize return & return answer

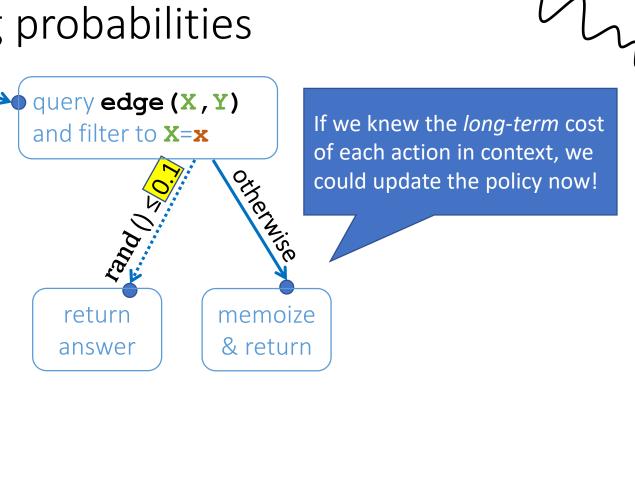


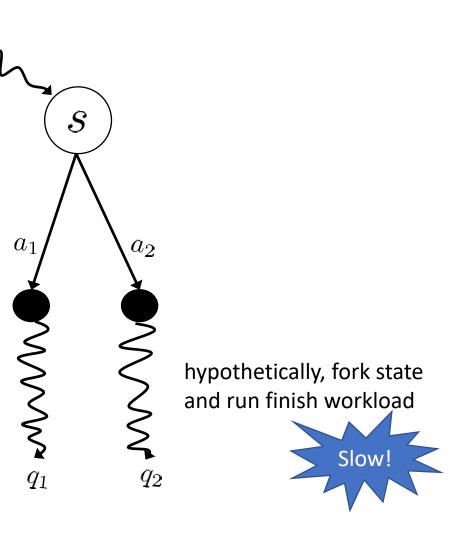
hypothetically, fork state and run finish workload

 a_1

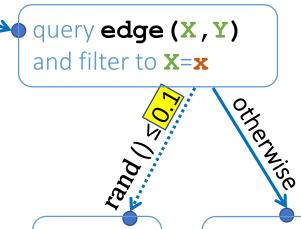
 q_1

 a_2





Tuning probabilities



return

answer

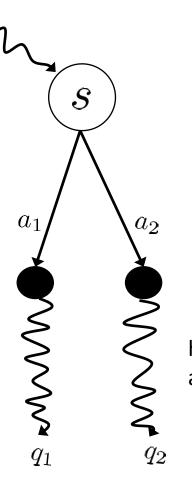
If we knew the *long-term* cost of each action in context, we could update the policy now!

Use ML to predict future costs!



memoize

& return



hypothetically, fork state and run finish workload



Tuning probabilities query **edge (X,Y)** If we knew the long-term cost and filter to X=x of each action in context, we could update the policy now! return memoize & return answer Generalize from past experience to new Use ML to predict situations future costs!

 a_1 a_2 hypothetically, fork state and run finish workload Slow! q_1

Tuning probabilities

query **edge (X,Y)** and filter to **X=x**

return

If we knew the *long-term* cost of each action in context, we could update the policy now!

Generalize from past experience to new situations

memoize

& return

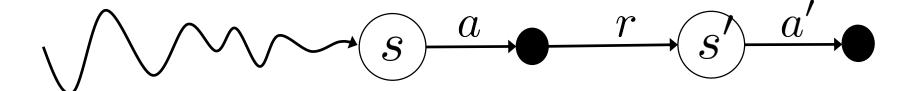
 a_1 a_2 q_1

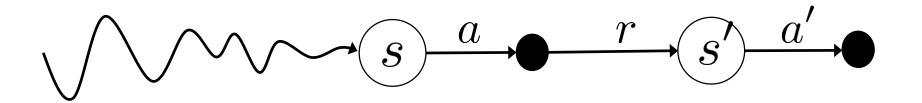
hypothetically, fork state and run finish workload



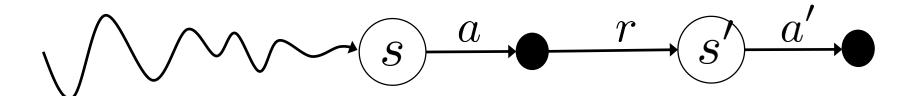
Use ML to predict future costs!

$$\mathbb{E}\left[q_i\right] \approx \widehat{q}(s, a_i) = w^{\top} \Phi(s, a_i)$$



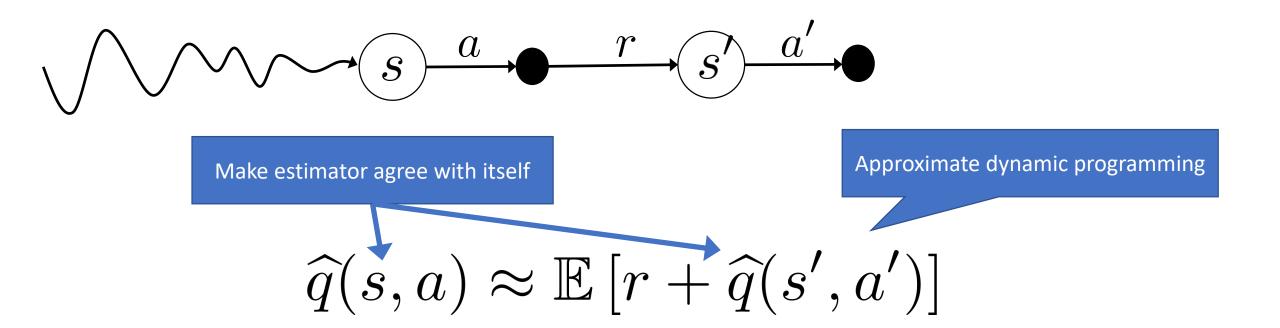


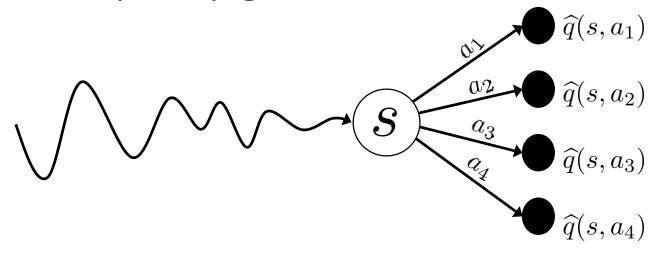
$$\widehat{q}(s,a) \approx \mathbb{E}\left[r + \widehat{q}(s',a')\right]$$

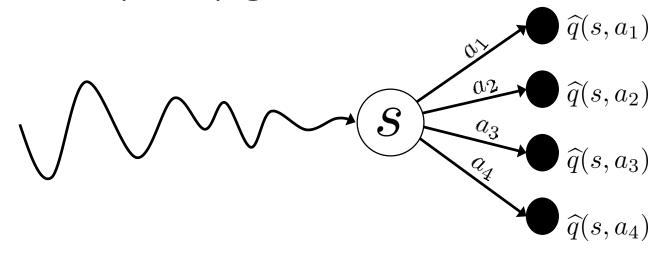


Approximate dynamic programming

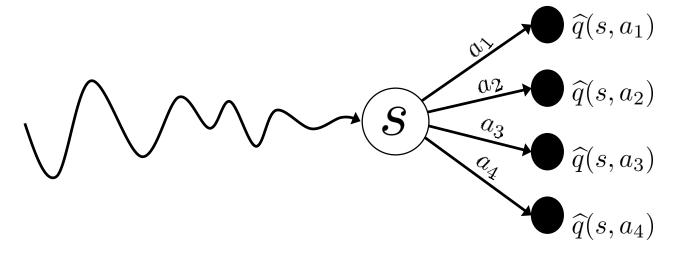
$$\widehat{q}(s,a) \approx \mathbb{E}\left[r + \widehat{q}(s',a')\right]$$







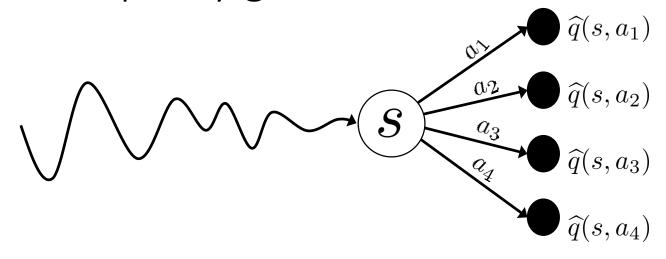
$$\pi(a|s) \propto \exp\left(\theta^{\top} f(s,a)\right)$$



 $\pi(a|s) \propto \exp\left(heta^ op f(s,a)
ight)$ of lower cost actions.

Says increase the probability

$$\theta \leftarrow \theta - \alpha_t \cdot \widehat{q}(s, a) \nabla \log \pi(a|s)$$

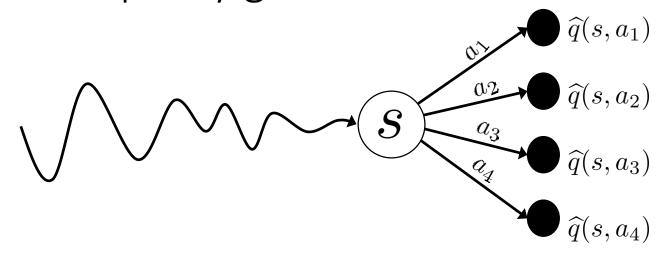


$$\pi(a|s) \propto \exp\left(\theta^{\top} f(s,a)\right)$$

$$\theta \leftarrow \theta - \alpha_t \cdot \widehat{q}(s, a) \nabla \log \pi(a|s)$$

Says increase the probability of lower cost actions.

$$\pi(\cdot|s) \approx \underset{a'}{\operatorname{argmin}} \ \widehat{q}(s,a')$$



$$\pi(a|s) \propto \exp\left(\theta^{\top} f(s,a)\right)$$

 $\theta \leftarrow \theta - \alpha_t \cdot \widehat{q}(s, a) \nabla \log \pi(a|s)$

update q

Says increase the probability of lower cost actions.

$$\pi(\cdot|s) \approx \underset{a'}{\operatorname{argmin}} \ \widehat{q}(s,a')$$

$$w = w - \beta_t \cdot (\widehat{q}(s, a) - (r + \widehat{q}(s', a'))) \cdot \Phi(s, a)$$

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 - Has been designed from the ground up be as flexible as possible.
 - A powerful language for specifying machine learning applications.

Check out the paper! Lots of great technical details in the paper that didn't have time to get into.

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 - Dyna 1 prototype (2005) was used in Jason's lab, fueling a dozen NLP papers!
 - Dyna 2 prototype (2013) was used for teaching an NLP course to linguists with no programming background.
- Both were inefficient because they used too many one-size-fits-all strategies.

Thanks!

Questions? Comments?



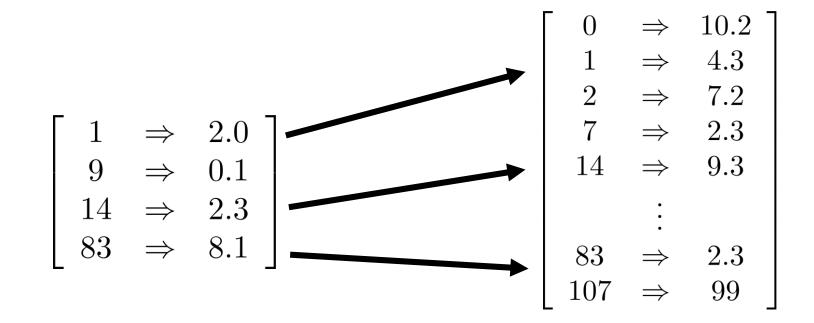
Hire Wes Filardo!
http://cs.jhu.edu/~nwf

http://dyna.org



@xtimv
@matthewfl

Loop order, sparse vector product example



Join strategies

- Outer loop on b (J, 4), inner loop a (I, J)
- Outer loop on a (I, J), inner loop b (J, K), filter K==4
- Sort **a** and **b** on **J** and use Baeza-Yates intersection
- What if we can't loop over b? e.g.,
 b(I,K) = X*Y.
- In natural language parsing with the CKY algorithm, an unexpected loop order turned out to be 7-9x faster than the loop order presented in most textbooks because of cache locality (Dunlop et al. 2010).

```
% matrix multiplication
c(I,K) += a(I,J) * b(J,K).
```

Memoization and data structures

- Do we store results for future use? (tradeoff: memos must be kept up-to-date!)
- What data structure?

Batching, answering bigger queries/updates

- Batch pending **c** queries.
- Preemptively compute a broader query, c(I,K)
 Use clever mat-mul alg. (sparse or dense?)

Inlining

- Inline a and/or b queries.
- Bypass agenda and route directly to consumer, e.g.,
 d(I) max= c(I,K).
- Reduce overhead of method calls
- Reduce overhead of task indirection through agenda

Mixed policies

- Mixed <u>task</u> strategies selection
 - Policy will encounter similar tasks frequently
- Mixed storage strategies
 - e.g., use a hash table, prefix trie, dense array, ...
 - Problem: random choice of strategy might not be consistent
 - E.g. might write to A and read from B (because of randomness)

Storage

Implementations?

Hash cons, trie (different orders on keys), dense vs. sparse, sorted (what to sort on)

Queries

What's the weight of edge a->b
Outgoing edges from a
Incoming edges to b
List all edges

List all self loops

Edges with weight >= 10

- ? edge("a", "b")
- ? edge("a",Y)
- ? edge (X, "b")
- ? edge (X, Y)

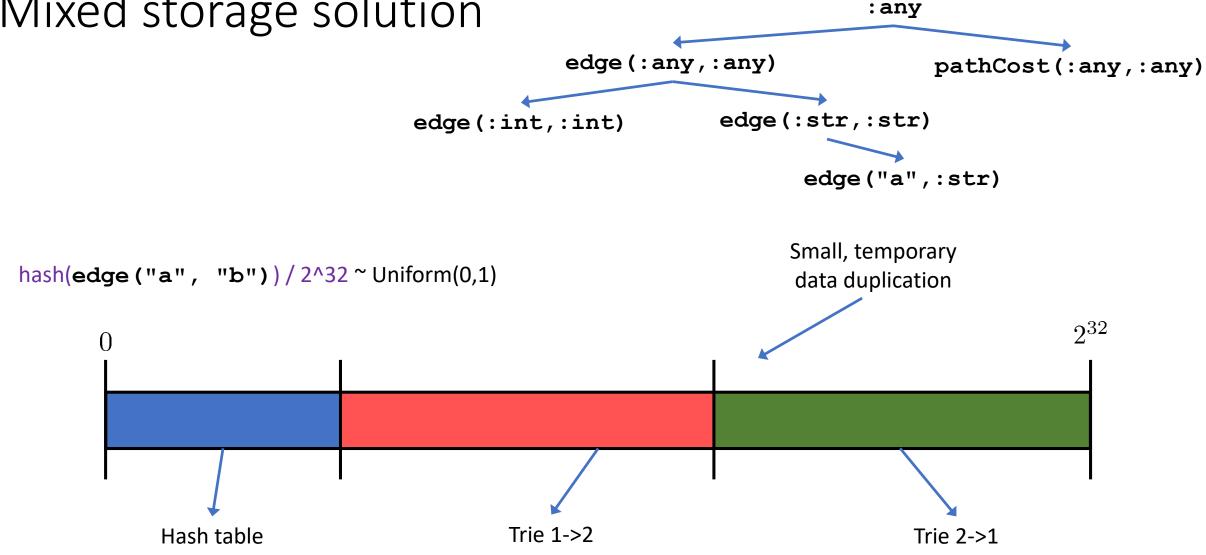
key

- ? edge (X,X)
- ? edge (X,Y) >= 10

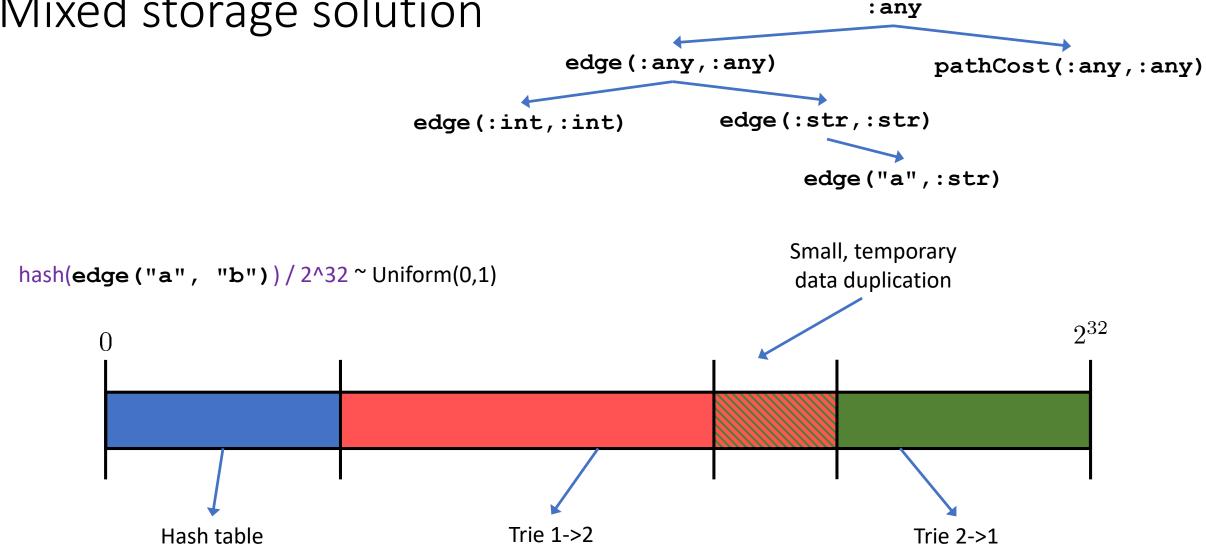
Efficiency depends on

- Frequency of different queries
- Overhead of read/writes
- Sizes
- Lower-level thresholds

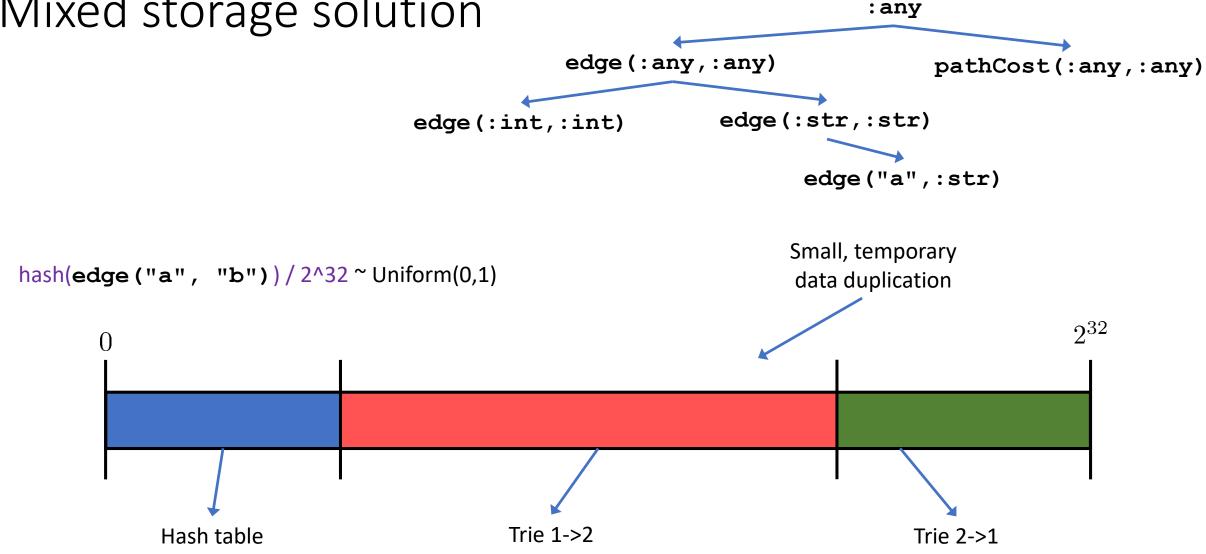
Mixed storage solution



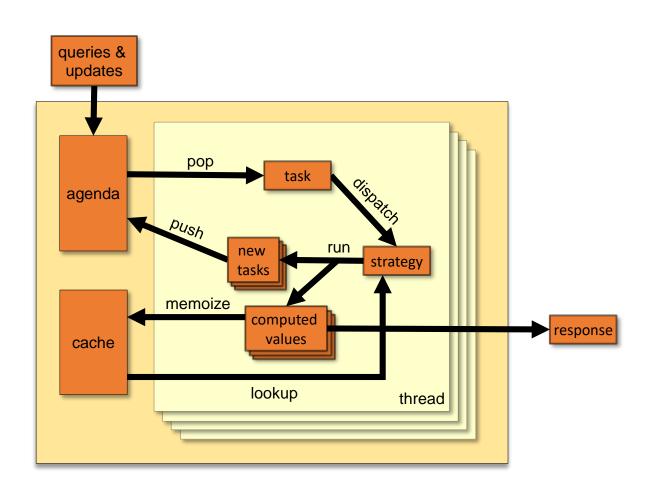
Mixed storage solution



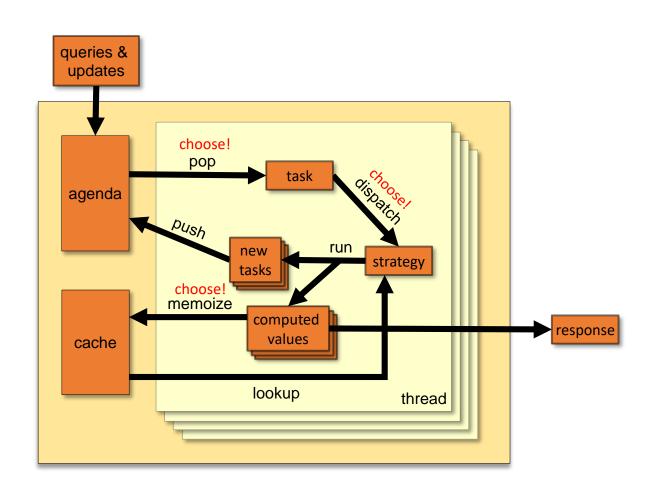
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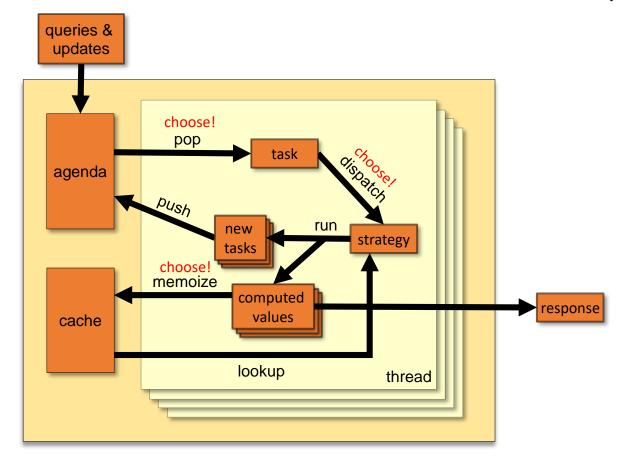
Learning to choose a good strategy

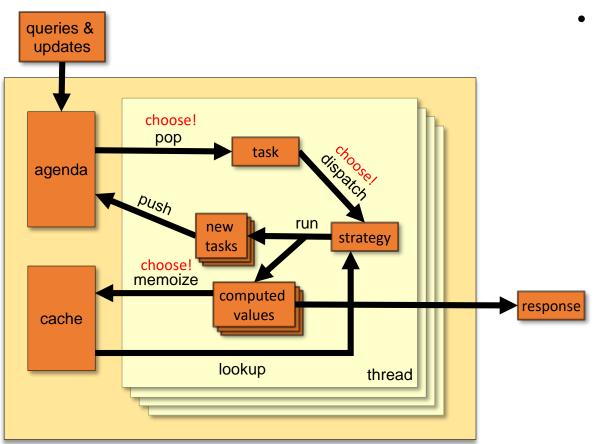


Learning to choose a good strategy

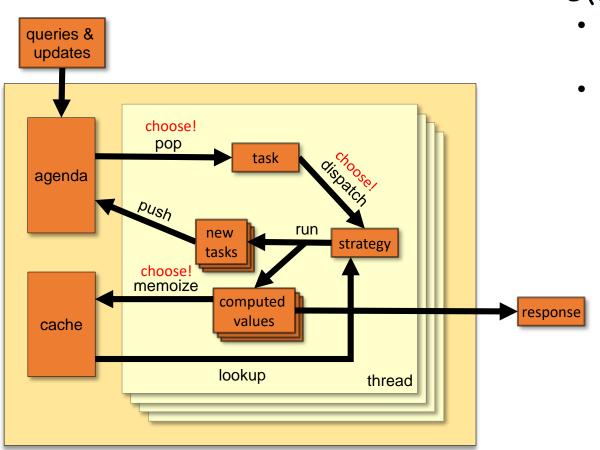


1. Bandit: Each time we execute a task (e.g., computec(I,j) for an argument j):

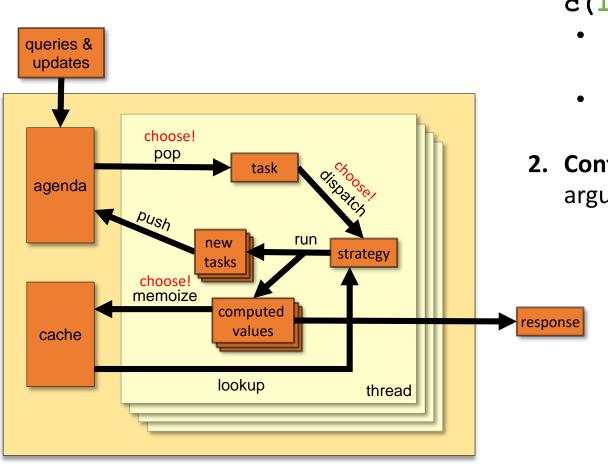




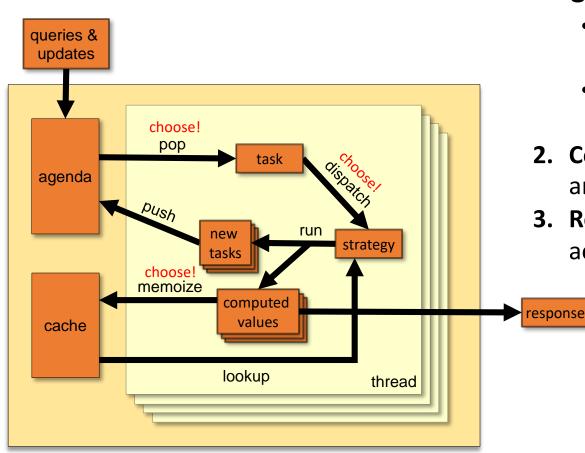
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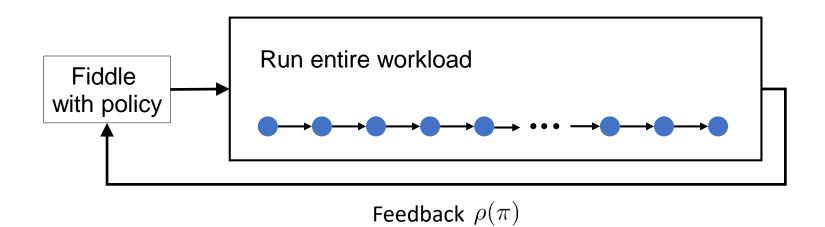
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- **2. Contextual bandit**: Allows distribution to depend on task arguments (e.g., j) and solver state.
- **3. Reinforcement learning**: Accounts for *delayed* costs of actions.

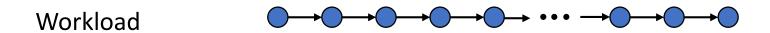
Back to online training...

Back to online training...

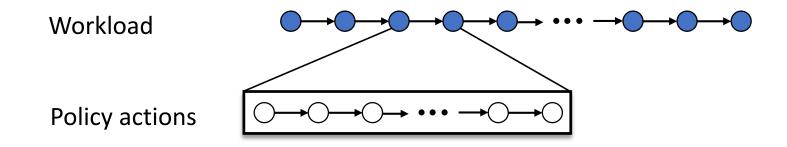


Solver Actions

Solver Actions

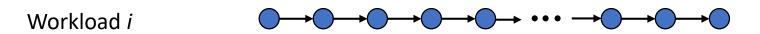


Solver Actions



TODO inline in parens use underbrace to give it a name

Add Jason integral picture?



TODO inline in parens use underbrace to give it a name

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Workload i



$$\rho(\pi) = \mathbb{E}\left[\sum_{i=1}^{\infty} \gamma^i \lambda_i \operatorname{latency}(i)\right]$$

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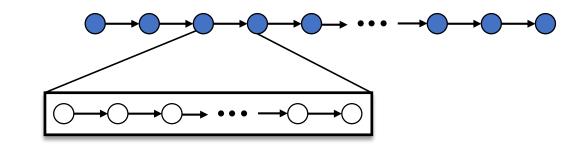
$$\rho(\pi) = \mathbb{E}\left[\sum_{i=1}^{\infty} \gamma^i \lambda_i \operatorname{latency}(i)\right] \quad \operatorname{Actions} t$$

Workload i

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$$ho(\pi) = \mathbb{E}\left[\sum_{i=1}^{\infty} \gamma^i \lambda_i \operatorname{latency}(i)
ight]$$
 Actions t

Workload i



$$= \mathbb{E}\left[\sum_{t=1}^{\infty} \operatorname{load}(t) \cdot (\operatorname{clock}(t+1) - \operatorname{clock}(t))\right] -$$

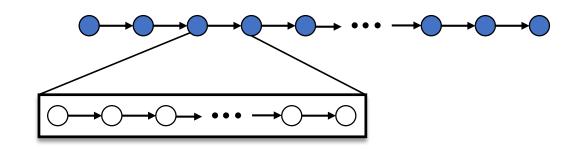
Rewrite in terms of the policy's time scale (used in RL)

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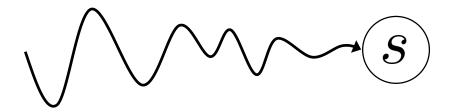
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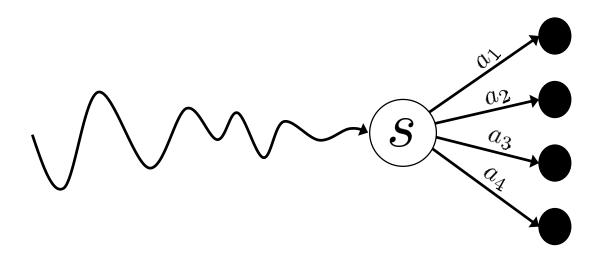
Each step tries to decrease the load

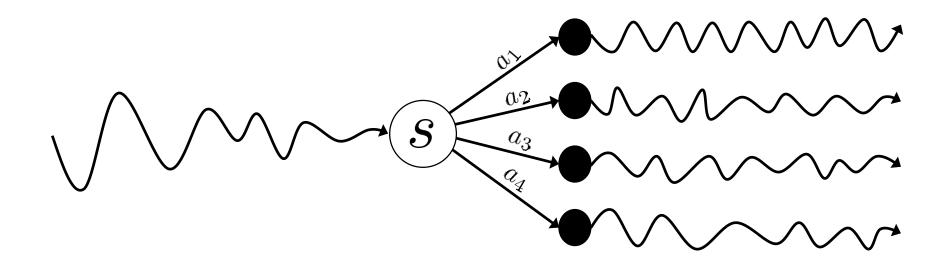
$$\operatorname{load}(t) = \sum_{i \in \mathcal{O}(t)} \gamma^i \lambda_i$$

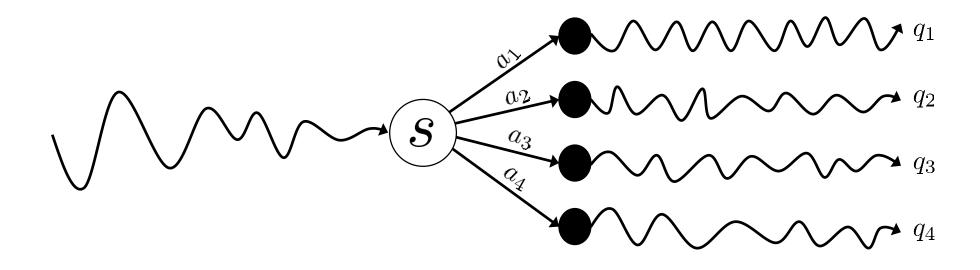
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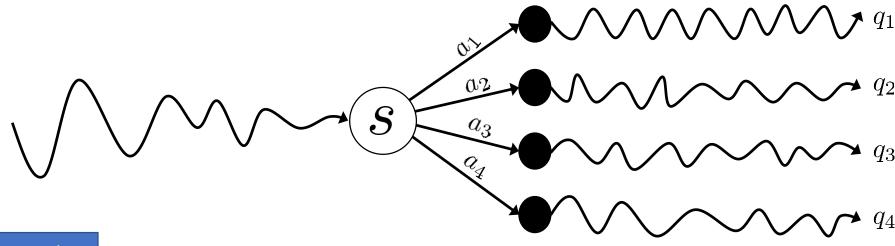
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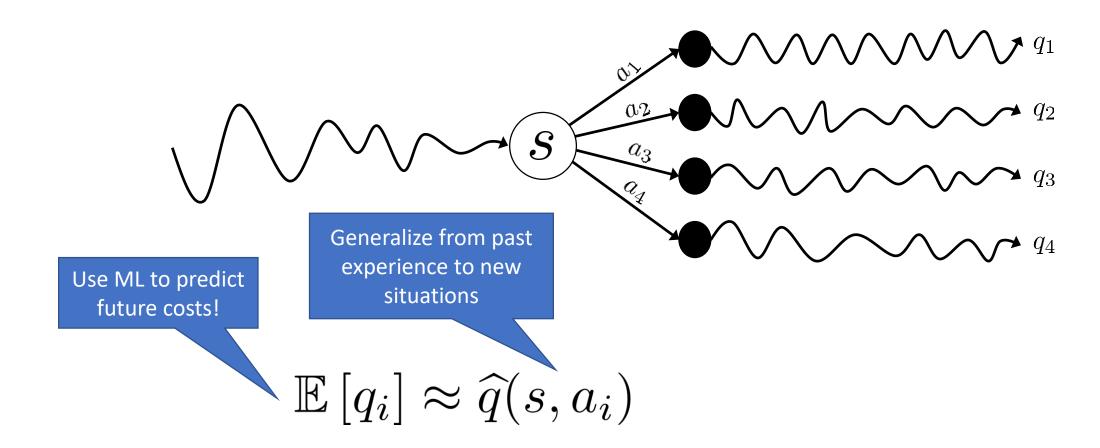


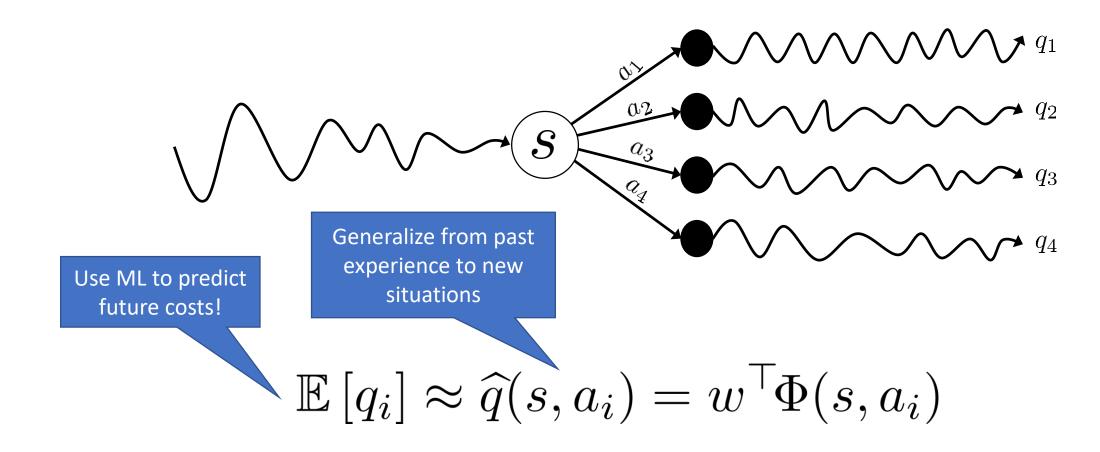


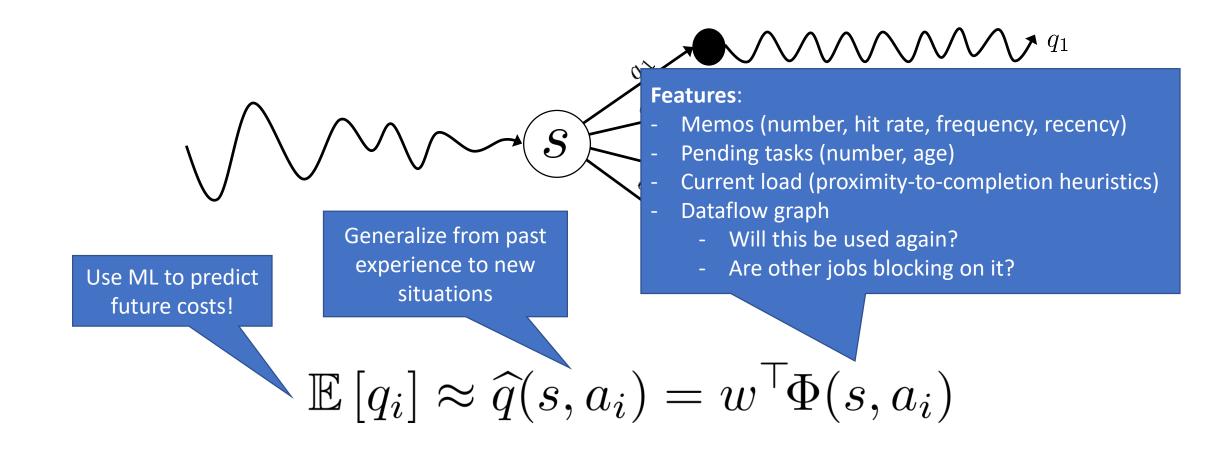


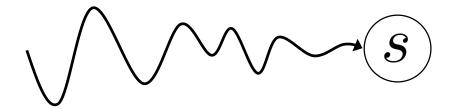
Use ML to predict future costs!

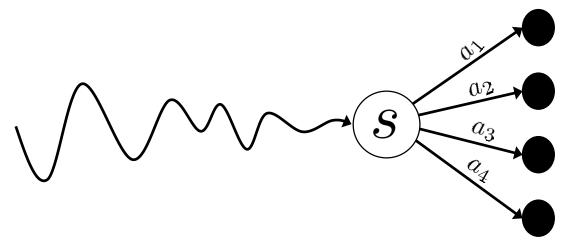
$$\mathbb{E}\left[q_i\right] \approx \widehat{q}(s, a_i)$$



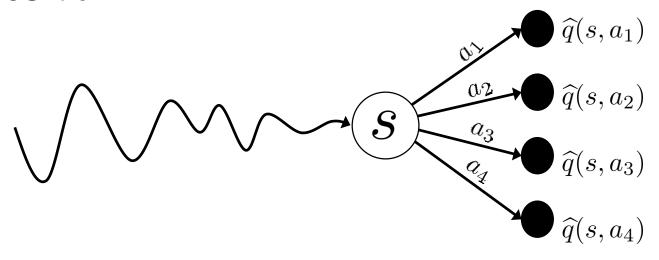


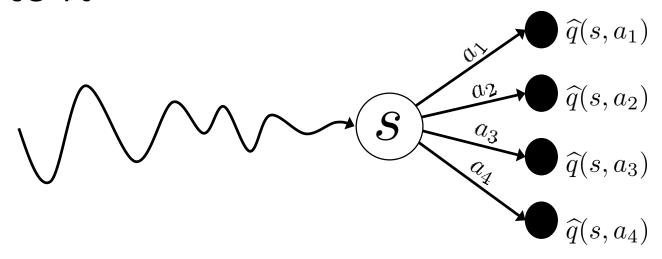




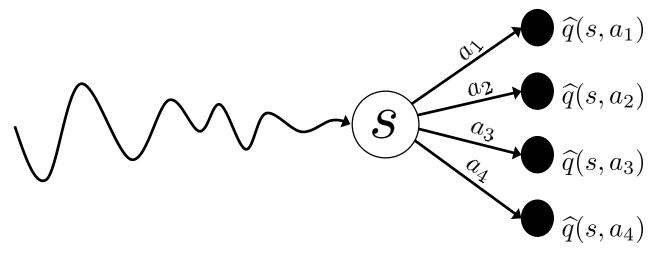


Back to π



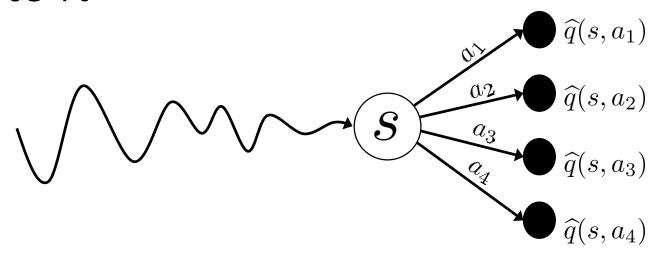


What should π do in this state?



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$$\pi(s) = \underset{a}{\operatorname{argmin}} \ \widehat{q}(s, a)$$

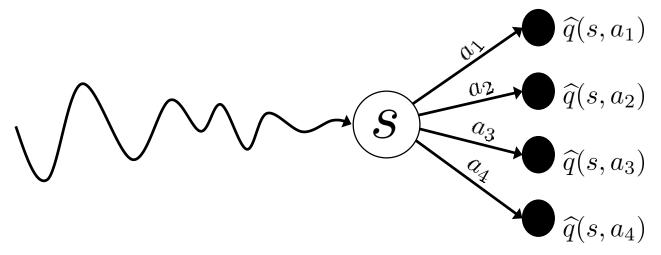


What should π do in this state?

$$\pi(s) = \underset{a}{\operatorname{argmin}} \ \widehat{q}(s, a)$$

Predicting the future requires richer features than simply learning to take good actions.

Back to π

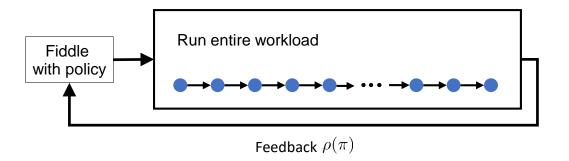


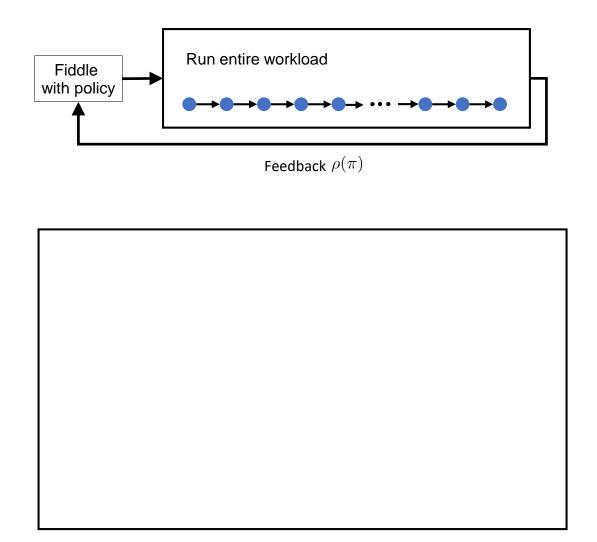
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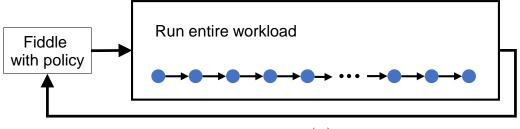
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Predicting the future requires richer features than simply learning to take good actions.

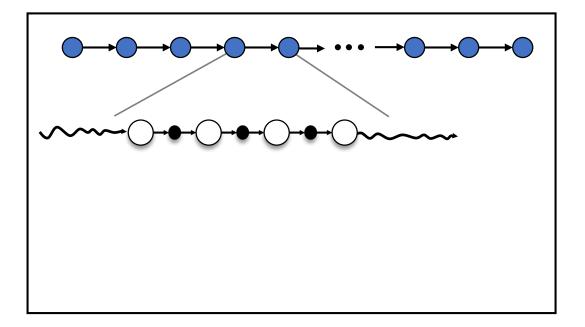
We need π to be really fast to execute!

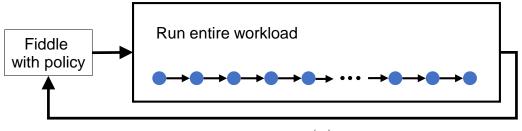






Feedback $ho(\pi)$





Feedback $\rho(\pi)$

